

James Brown's

Book

May 8th 1808

LB

James Brown

Born July 30 1790

+

Simple Addition

Examples

$$\begin{array}{r} 843764583 \\ 276357830 \\ 632858876 \\ 453868158 \\ 344500880 \\ \hline 2551022141 \\ 1707257538 \\ \hline 2551022141 \end{array}$$

$$\begin{array}{r} 34567892 \\ 41034560 \\ 12345676 \\ 21008417 \\ 56145682 \\ \hline 165102221 \\ 130534329 \\ \hline 165102221 \end{array}$$

Simple Subtraction

Examples

<p> $\begin{array}{r} \text{From } 1009400 \\ \text{Take } 9411 \\ \hline 999789 \\ 1009400 \text{ Answer} \end{array}$ </p>	<p> $\begin{array}{r} \text{From } 50500041 \\ \text{Take } 34125678 \\ \hline 16474363 \\ 50600041 \text{ Answer} \end{array}$ </p>
---	---

Simple Multiplication

Examples

Multiply 167894 by 16

$$\begin{array}{r} 167894 \\ 16 \\ \hline 1007364 \\ 167894 \\ \hline 2586304 \text{ proof} \end{array}$$

Multiply 4312589 by 183

$$\begin{array}{r} 4312589 \\ 183 \\ \hline 12938067 \\ 34501512 \\ 4312689 \\ \hline 789222087 \end{array}$$
 6/0.
0/3.
proof

5/5

Continued

Multiply 14673167456 by 3452142

$$\begin{array}{r}
 14673167456 \\
 \times 3452142 \\
 \hline
 29346334912 \\
 58692669824 \\
 14673167456 \\
 29346334912 \\
 58692669824 \\
 58692669824 \\
 44019502368 \\
 \hline
 5064457647990752
 \end{array}$$

Multiply 264648436 by 3699604

$$\begin{array}{r}
 1058593744 \\
 1587890616 \\
 2391835924 \\
 793945308 \\
 1588790616 \\
 793945308 \\
 \hline
 983215506239344
 \end{array}$$

~~7/11~~ Proof

Simple Division

Examples

Divide 859673 by 57656

$$\begin{array}{r}
 57656 \overline{) 859673} \text{ Answer} \\
 \underline{57656 \times} \\
 283113 \\
 \underline{2830624 \times} \\
 524897
 \end{array}$$

859673 Proof

Continued

3

A farm of 375 Acres is let for 1125 how much does it
pay per Acre

$$375 \overline{) 1125} \text{ (3 Answer 3 Dollars)}$$

So many number of men were concerned in
the payment of 18950 Dollars and each
man paid 25 Dollars what was the number
of men

$$\begin{array}{r} 25 \overline{) 18950} \text{ (758 Ans 758 Dollars)} \\ \underline{175} \\ 145 \\ \underline{125} \\ 200 \\ \underline{200} \end{array}$$

What number must I multiply by 13 that
the product may be 891

$$\begin{array}{r} 13 \overline{) 891} \text{ (69 Ans 69)} \\ \underline{78} \\ 91 \\ \underline{91} \end{array}$$

An Army of 15000 men having plundered
A City took 2625000 Dollars what was
each mans share

$$\begin{array}{r} 15000 \overline{) 2625000} \text{ (175 Answer 175 Dollars)} \\ \underline{15} \\ 112 \\ \underline{105} \\ 75 \\ \underline{75} \end{array}$$

Compound Addition

Examples

Suppose A man goes a journey and on the first day

14 02	May 14 th pays for dinner	— 0 = 1 = 6
	for cart for his horse	— 0 = 0 = 6
	for shoe	— 0 = 1 = 2
	for supper and lodging	0 = 2 = 0
	for horse keeping	0 = 1 = 10
	for betters	0 = 1 = 6
	for breakfast	0 = 2 = 0
	to the barber for dressing	0 = 1 = 6
	for dinner again and	0 = 3 = 5
	other refreshments	£ 0 = 15 = 5 Answer

A man purchases cattle one yoke of oxen for
 £ 14 = 11 = 6 four cows £ 18 = 19 = 7 and other
 stock to the amount of 21 £ = 5 what
 was the amount of the cattle purchased

£	0	0
14	= 11	= 6
18	= 19	= 7
21	= 05	= 0
£ 54	= 16	= 1 Answer

Troy Weight

Examples

#	oz	part	gr
784	= 11	= 19	= 23
457	= 8	= 14	= 22
674	= 7	= 13	= 14
684	= 7	= 12	= 13
<hr/>			
2602	= 0	= 1	= 0
1817	= 0	= 1	= 1
<hr/>			
2602	= 0	= 1	= 0

Avoirdupois Weight

Examples

Cwt	Lbs	to	oz	gr	Cwt	Lbs	to	oz	gr
28	= 3	= 22	= 13	= 13	33	= 3	= 12	= 8	= 2
13	= 2	= 18	= 12	= 13	12	= 2	= 13	= 4	= 1
68	= 1	= 21	= 11	= 16	13	= 3	= 18	= 6	= 3
<hr/>					<hr/>				
111	= 0	= 7	= 6	= 10	60	= 1	= 16	= 2	= 6
82	= 0	= 12	= 8	= 13	26	= 2	= 3	= 10	= 4
<hr/>					<hr/>				
111	= 0	= 7	= 6	= 10	60	= 1	= 16	= 2	= 6

Time

Examples

Month	& Weeks	Days
3	= 2	= 6
6	= 3	= 4
3	= 2	= 5
9	= 2	= 3
7	= 3	= 4
6	= 2	= 2
<hr/>		
2	= 12	= 1 = 3
2	= 8	= 2 = 4
<hr/>		
2	= 12	= 1 = 3

Cloth Measure

Examples

$$17 = 3 = 3$$

$$26 = 2 = 2$$

$$18 = 2 = 3$$

$$46 = 3 = 0$$

$$34 = 0 = 2$$

$$53 = 2 = 2$$

$$197 = 3 = 0$$

$$177 = 8 = 1$$

$$197 = 3 = 0$$

$$14 = 3 = 1$$

$$29 = 2 = 2$$

$$49 = 2 = 3$$

$$36 = 3 = 2$$

$$47 = 3 = 1$$

$$36 = 2 = 0$$

$$234 = 3 = 1$$

$$200 = 0 = 0$$

$$234 = 3 = 1$$

Long Measure

Examples

Yds Miles St Rods Yds Feet Inches

$$19 = 58\frac{1}{2} = 9 = 39 = 4\frac{1}{2} = 2 = 11$$

$$37 = 13\frac{1}{2} = 6 = 27 = 3\frac{1}{2} = 2 = 9$$

$$22 = 14 = 2 = 21 = 4 = 0 = 5$$

$$92 = 19 = 6 = 31 = 3 = 1 = 3$$

$$171 = 39\frac{1}{2} = 0 = 1 = \frac{1}{2} = 1 = 4$$

$$151 = 48\frac{1}{2} = 0 = 1 = \frac{1}{2} = 1 = 5$$

$$171 = 39\frac{1}{2} = 0 = 1 = \frac{1}{2} = 1 = 4$$

Land or Square Measure

Examples

Acres	¹⁰⁰ Rod	¹⁶⁰ Pole	Feet	Inches
396	= 3	= 36	= 93	= 721
568	= 1	= 27	= 58	= 76
249	= 2	= 35	= 81	= 24
1193	= 0	= 18	= 213	= 77
816	= 0	= 22	= 119	= 100
1193	= 0	= 18	= 213	= 77

Solid Measure

Examples

Cord	Feet	Inches
39	= 118	= 1021
3	= 56	= 437
18	= 72	= 659
29	= 86	= 724
91	= 92	= 113
57	= 86	= 1220
91	= 92	= 113 Proof

Dry Measure

Examples

Weg

Coorn

bu

pk

Quarts

$$189 = 9 = 3 = 3 = 9$$

$$843 = 8 = 2 = 2 = 6$$

$$745 = 9 = 3 = 3 = 6$$

$$987 = 8 = 3 = 3 = 5$$

$$668 = 7 = 3 = 2 = 9$$

$$848 = 6 = 3 = 3 = 4$$

$$4883 = 2 = 2 = 0 = 1 \text{ Answer}$$

$$4095 = 2 = 2 = 0 = 2$$

$$4883 = 2 = 2 = 0 = 1 \text{ Proof}$$

Compound Subtraction

Examples

Len 4 185 = 10 = 7
 Received = 93 = 15 = 0
 Due 91 = 15 = 7
 Proof 185 10 = 7

4 10
 Answer 310 = 0
 Take 85 = 15
 224 = 5 Ans
 310 = 0 Proof

Troy Weight

Examples

lb 3 part gr
 Answer 76 = 8 = 16 = 13
 Take 3 = 9 = 19 = 6

$$\text{Answer } 72 = 10 = 19 = 7$$

$$\text{Proof } 76 = 8 = 16 = 13$$

Arithmetical Weight

Examples

From $\frac{3}{4}$ Tuns $\frac{3}{4}$ Tuns
 Take $9 = 9 = 12$
 Take $3 = 12 = 9$

$$3 = 13 = 3$$

$$4 = 0 = 14$$

$$9 = 9 = 12$$

$$8 = 2 = 13$$

Cloth Measure

Examples

	Yds	Qu	Nailes	Ell	In	Nailes
From	27	=	7	=	2	
Take	16	=	1	=	3	
	10	=	3	=	3	
	27	=	1	=	2	

$$26 = 2 = 1$$

$$17 = 3 = 2$$

$$8 = 3 = 3$$

$$26 = 2 = 1$$

Long Measure

Examples

Yds	Ells	Tuns	Sp	Yds	Ells	In	Tuns	
56	=	13	=	5	=	26	=	2
17	=	15	=	2	=	27	=	1

$$38 = 6\frac{1}{2} = 2 = 39 = 0 = 1 = 10 = 2$$

$$56 = 13 = 5 = 26 = 2 = 1 = 8 = 1$$

Square or Square Measure

Examples

From	Yds	Ells	Take	Yds	Ells	Take
17	=	7	=	17	=	16
16	=	1	=	16	=	16

$$1 = 0 = 1$$

$$16 = 1 = 16$$

Solid Measure

Examples

$$\begin{array}{rcl} \text{From } 49 & - & 29 & = & 186 \\ \text{Take } 19 & = & 34 & = & 1237 \\ \hline 29 & = & 122 & = & 677 \\ \hline 49 & = & 29 & = & 186 \end{array}$$

set 12

Dry Measure

Examples

$$\begin{array}{rcl} \text{From } 61 & - & 1 & = & 2 \\ 5 & - & 1 & = & 4 \\ \hline 55 & = & 3 & = & 6 \text{ Answer} \\ \hline 61 & = & 1 & = & 2 \text{ Proof} \end{array}$$

Reduction Descending

Examples

Q. In 23471 half pence how many pence?

$$\begin{array}{r} 2 \overline{) 23471} \\ \underline{11735} \\ 11735 \\ \underline{108} \\ 93 \\ \underline{86} \\ 95 \\ \underline{86} \\ 11 \end{array}$$

Answer 48 \pm 17 = 11 $\frac{1}{2}$

Q. In 63 Guineas at 28 Pence each how many six pence?

$$\begin{array}{r} 63 \\ \underline{28} \\ 506 \\ \underline{126} \\ 1764 \\ \underline{2} \\ 3528 \text{ Answer} \end{array}$$

Continued

11

1st In 37 Dollars how many half pence

$$\begin{array}{r}
 37 \\
 \underline{6} \\
 222 \\
 \underline{12} \\
 114 \\
 \underline{222} \\
 2664 \\
 \underline{2} \\
 5328 \text{ Ans}
 \end{array}$$

2^d In 1137 how many 1/2 pence

$$\begin{array}{r}
 16 \\
 \underline{222} \\
 37 \\
 \hline
 592 \text{ Ans}
 \end{array}$$

4th How often will a wheel of 16 1/2 feet circumference turn round in the distance from Newburyport to Cambridge it being 42 miles

$$\begin{array}{r}
 42 \\
 \underline{8} \\
 336 \\
 \underline{40} \\
 2 \overline{)13440} \\
 \underline{16} \\
 80640 \\
 \underline{13440} \\
 215040 \\
 \underline{6720} \\
 221760 \\
 \underline{2} \\
 221762
 \end{array}$$

$$\begin{array}{r}
 16 \frac{1}{2} \\
 \underline{33}
 \end{array}$$

$$\begin{array}{r}
 33 \overline{)443520} \quad (13440 \text{ Answer} \\
 \underline{33} \\
 113 \\
 \underline{99} \\
 245 \\
 \underline{132} \\
 132 \\
 \underline{132} \\
 0
 \end{array}$$

Continued

Q. In 49 £ 15 S 4 how many Dollars and cents

$$\begin{array}{r} 3/490000 \\ 16333 \end{array}$$

$$\begin{array}{r} 6/15000 \\ 2500 \end{array}$$

$$\begin{array}{r} 3/4000(55 \\ 160 \\ 400 \\ 160 \\ 40 \end{array}$$

$$\begin{array}{r} 165 = 33-9 \\ 2 = 50-0 \\ 5-5 \end{array}$$

$$165 = 88 = 8 \text{ Answer}$$

Q. In 54 guineas how many pounds Dollars and shillings of each an equal number

$$\begin{array}{r} 54 \\ 28 \\ 432 \\ 108 \end{array}$$

$$\begin{array}{r} 20 \\ 1 \\ 29 \text{ Division} \end{array}$$

$$\begin{array}{r} 29 \overline{) 151256} \\ 135 \\ \hline 162 \\ 162 \end{array} \text{ Answer}$$

Q. In 192 pounds how many eagles Dollars and ninepences of each the like number

$$\begin{array}{r} 10 \text{ eagles} \\ 1000 \\ 100 \\ 125 \\ \hline 11125 \\ 2225 \end{array}$$

$$\begin{array}{r} 192 \\ 132 \\ 1032 \\ 516 \\ \hline 6/192000(\text{shillings} \\ 1032000 \\ 100 \\ \hline 103200 \end{array}$$

$$2225 \overline{) 20025} \text{ Answer } 92 \text{ of each}$$

$$\begin{array}{r} 6/50 \\ 4450 \\ \hline 25 \overline{) 1000} \end{array} \text{ and 68 ninepences}$$

J. & W. Weight Co

Examples

9th Ex. 35 $\frac{1}{12}$ lb how many grains

$$\begin{array}{r}
 708 \\
 354 \\
 \hline
 4248 \\
 20 \\
 \hline
 84960 \\
 24 \\
 \hline
 339840 \\
 169920 \\
 \hline
 2039040
 \end{array}$$

Ex 40 $\frac{1}{12}$ lb of Silver how many
table spoons weighing 22 part
each and how many
3 part Spooner's each can be made
and an equal number of each

$ \begin{array}{r} 47 \\ 12 \\ \hline 564 \\ 20 \\ \hline 11280 \\ 24 \\ \hline 45120 \\ 22560 \end{array} $	$ \begin{array}{r} 22 \\ 3-6 \\ \hline 25-6 \\ 24 \\ \hline 108 \\ 50 \\ \hline 608 \end{array} $
--	--

$$\begin{array}{r}
 806 \overline{) 270720} (446 \\
 \underline{2424} \\
 2832 \\
 \underline{2424} \\
 4080 \\
 \underline{3636} \\
 24 \overline{) 444} (18 \\
 \underline{24} \\
 204 \\
 \underline{192} \\
 12
 \end{array}$$

Answer 446 of each
sort and 18 part
Spooner's over

Indulpois Weight Examples

1st In 24 - 19 = 5 - 19 = 5 - 14

20

497

1

1791

28

15735

3983

55765

16

354595

55765

572245

16

5553494

572245

14295724

2nd In 4976 Drums how many pounds

16/4976 (298/18)

32

16

157

138

144

128

136

10

128

8

Answer 18 lbs 10 oz 8 Drums

Spithecary Weight Examples

1st In 12 to 933 how many grains

12

153

4

1224

3

3672

20

93440

2nd In 93440 grains how many pounds

20/93440

3) 3672

8) 1224

12) 153

12-9

Answer 12 - 9

Scotch Measure

Examples

Ques In 596 ells how many yards

$$\begin{array}{r} 4 \overline{) 23840} \\ \underline{19520} \\ 4320 \end{array} \text{ Ans}$$

How many weth can be made of 27 yds 19 yards
allowing 7 yds for a weth

$$\begin{array}{r} 27 = 1 \\ 7 \overline{) 109} \text{ (15)} \\ \underline{35} \\ 74 \\ \underline{70} \\ 4 \end{array}$$

Answer 15 weth 2. Yards 2. over

Dry Measure

Examples

In 49 bushels how many quarts

$$\begin{array}{r} 4 \overline{) 196} \\ \underline{156} \\ 40 \end{array} \text{ Ans}$$

Liquid Measure

Examples

1st In 3 hogsheads how many gills

$$\begin{array}{r} 3 \\ 23 \\ 179 \\ 4 \\ \hline 956 \\ 2 \\ \hline 1512 \\ 4 \\ \hline 5048 \text{ Ans} \end{array}$$

2nd How long will A barrel of wine last if you draw 6 quarts per day

$$\begin{array}{r} 4 \\ 6 \overline{)126} (21 \text{ Answer} \\ 12 \\ \hline 6 \\ \hline 6 \end{array}$$

3rd How many Apples will it take to make A load or ton allowing 3 Apples to make A gill

$$\begin{array}{r} 4 \\ 63 \\ 252 \\ 4 \\ \hline 1008 \\ 8 \\ \hline 8064 \\ 3 \end{array}$$

24192 Ans

4th In 88 Gallons how many vells

$$\begin{array}{r} 88 \\ 11 \overline{)176} \\ 16 \text{ Answer} \end{array}$$

5th How many inches is A mile

$$\begin{array}{r} 4 \\ 40 \\ 2 \overline{)320} \\ 26 \\ \hline 120 \\ 52 \\ \hline 5120 \\ 160 \\ \hline 5280 \\ 12 \end{array}$$

5280 Answer

Time

Examples

1st Supposing A man to be 21 years old how many seconds has he liv'd allowing 365 Days 6 hours to the year

$$\begin{array}{r}
 \text{Days} \quad \text{hr} \\
 365 = 6 \\
 \underline{24} \\
 1466 \\
 730 \\
 \hline
 8766 \\
 21 \\
 \hline
 8766 \\
 17532 \\
 \hline
 184086 \\
 60 \\
 \hline
 11045160 \\
 60 \\
 \hline
 662709600 \text{ Seconds Answer}
 \end{array}$$

Long Measure

Examples

1st How many steps does a man take in going 4 mile if you step 2 feet 2 inches at a step

$$\begin{array}{r}
 \text{Feet} \quad \text{In} \\
 2 - 2 \\
 \underline{12} \\
 24
 \end{array}$$

$$\begin{array}{r}
 40 \\
 2 \overline{) 720} \\
 \underline{40} \\
 320 \\
 \underline{240} \\
 80 \\
 \underline{60} \\
 20 \\
 \underline{12} \\
 8 \\
 \underline{6} \\
 2
 \end{array}$$

$$\begin{array}{r}
 10560 (2436 \\
 \underline{5280} \\
 5280 \\
 \underline{5280} \\
 0
 \end{array}$$

Answer 2436 steps 2 inches over

Continued

The forward wheels of a wagon are $4\frac{1}{2}$ feet in circumference and the hind wheels 15 feet 9 inches how many more times will the forward wheels turn round than the hind ones in going 24 5 miles

$$\begin{array}{r} 24\frac{5}{8} \\ \hline 19\frac{4}{40} \end{array}$$

$$\begin{array}{r} 1\frac{1}{2} \\ \hline 29 \end{array}$$

$$\begin{array}{r} 15\frac{3}{4} \\ \hline 63 \end{array}$$

$$2 \overline{) 7936\frac{1}{2}}$$

$$\begin{array}{r} 396800 \\ 39680 \end{array}$$

$$\begin{array}{r} 436480 \end{array}$$

$$\begin{array}{r} 1309440 \end{array}$$

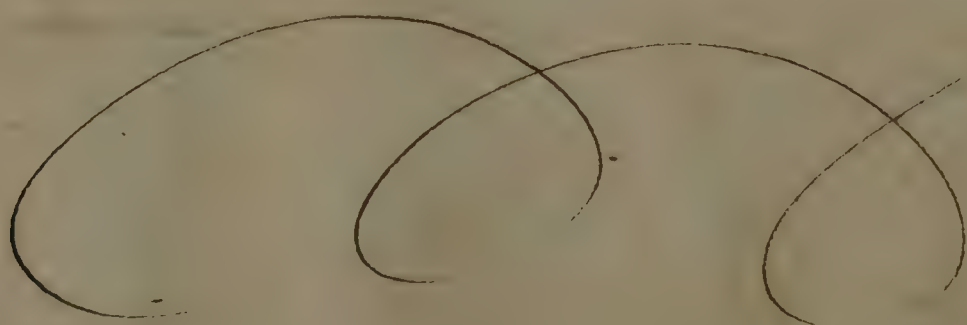
$$\begin{array}{r} 92618880 \end{array}$$

$$\begin{array}{r} 88 \\ 87 \\ \hline 180 \\ 174 \\ \hline 6 \\ \hline 29 \end{array}$$

$$\begin{array}{r} 1309440 \\ \hline 63 \overline{) 5237760} \end{array}$$

$$\begin{array}{r} 197 \\ 189 \\ \hline 89 \\ 83 \\ \hline 246 \\ 189 \\ \hline 570 \\ 567 \\ \hline 3 \\ \hline 63 \end{array}$$

The forward wheels turn round 90305 times
The hind wheels 7167 times Answer



29

Land or Square Measure

Examples

1st In one mile how many square rods

$$\begin{array}{r}
 320 \\
 320 \\
 \hline
 6400 \\
 960 \\
 \hline
 102400 \text{ Answer}
 \end{array}$$

2nd In a room 16 feet square how many square feet

$$\begin{array}{r}
 16 \\
 16 \\
 \hline
 96 \\
 16 \\
 \hline
 256 \text{ Ans}
 \end{array}$$

3rd How many acres in a field 36 rods long and 36 wide

$$\begin{array}{r}
 36 \\
 36 \\
 \hline
 1296 \\
 108 \\
 \hline
 160 \overline{) 1152} \quad 7 \text{ Answer } 7 \frac{1}{2} \text{ Acres} \\
 \underline{1120} \\
 32 \overline{) 32} \quad 1 \\
 \underline{32} \\
 0
 \end{array}$$

4th How many shingles will cover a house 40 feet long and 30 feet rafters allowing each shingle to be 4 inches wide and each course 6 inches the length of the rafters

$$\begin{array}{r}
 30 \\
 30 \\
 \hline
 60 \text{ the length of the house} \\
 40 \\
 \hline
 2400 \\
 144 \\
 \hline
 9600 \\
 4600 \\
 500 \\
 \hline
 145600
 \end{array}$$

$$\begin{array}{r}
 4 \\
 6 \\
 \hline
 24
 \end{array}$$
 one shingle covers 24 inches

$$\begin{array}{r}
 24 \overline{) 145600} \quad 14400 \text{ Answer} \\
 \underline{24} \\
 105 \\
 \underline{96} \\
 96 \\
 \underline{96} \\
 0
 \end{array}$$

Cubic Measure

Examples - 6

104 In + cords of wood how many other inches

$$\begin{array}{r}
 128 \\
 5 \\
 \hline
 640 \\
 1280 \\
 \hline
 5120 \\
 1280 \\
 4480 \\
 640 \\
 \hline
 1105920 \text{ Answer}
 \end{array}$$

2nd How many bricks 8 inches long 4 inches wide and 2½ inches thick will it take to build a house 44 feet long 40 feet wide and 20 feet high and the walls 12 inches thick

$$\begin{array}{r}
 44 \\
 \underline{12} \\
 528 \\
 \underline{240} \\
 21120 \\
 \underline{1056} \\
 126720 \\
 \underline{12} \\
 253440 \\
 \underline{126720} \\
 1520640 \\
 \underline{2} \\
 3041280
 \end{array}$$

$$\begin{array}{r}
 20 \\
 \underline{12} \\
 240 \\
 \underline{40} \\
 480 \\
 \underline{240} \\
 19200 \\
 \underline{560} \\
 115200 \\
 \underline{12} \\
 1382400 \\
 \underline{2} \\
 2764800 \\
 \underline{3041280} \\
 80 \overline{) 5806080} \quad 72576 \text{ Answer}
 \end{array}$$

$$\begin{array}{r}
 80 \\
 \underline{560} \\
 206 \\
 \underline{160} \\
 460 \\
 \underline{400} \\
 608 \\
 \underline{520} \\
 480 \\
 \underline{480}
 \end{array}$$

$$\begin{array}{r}
 8 \times 4 \times 2\frac{1}{2} \\
 \underline{4} \\
 2132\frac{1}{2} \\
 \underline{64} \\
 16 \\
 \underline{80} \text{ Divisor}
 \end{array}$$

Simple Rule of Three

Examples

1st If 6th of sugar cost 4/6 what will 30th cost

$$6 = 4 = 6 = 30$$

$$\begin{array}{r} 54 \quad 12 \quad 20 \\ 30 \quad 270 \quad (22) \\ 6 \overline{) 1620} \quad 24 \quad (20) \\ \underline{12} \quad \underline{24} \quad \underline{2} \\ 42 \quad 30 \\ \underline{42} \quad \underline{24} \\ 0 \quad 6 \end{array}$$

Answer £2 2/6

2nd If 15 yards of cloth cost 3/4 what will 2 yards cost

$$15 = 3 = 2$$

$$\begin{array}{r} 20 \\ 15 \overline{) 120} \\ \underline{120} \end{array}$$

3rd If 3 cost 2 yds of sugar cost 9/10 what will 1 cost 2 yds 10th

$$3 = 2 = 9 = 10 = 1 = 2 = 10$$

$$\begin{array}{r} 4 \quad 20 \quad 4 \\ 14 \quad 190 \quad 6 \\ 28 \quad 178 \quad 28 \\ 112 \quad 1520 \quad 48 \\ 28 \quad 1330 \quad 13 \\ 352 \quad 190 \quad 178 \end{array}$$

$$\begin{array}{r} 2460 \\ 2452 \\ \underline{108} \\ 112 \end{array}$$

Answer 4 £ 6 9 3/4

Continued

5th If 57 yards cost 69 £ what will 9 yards cost

$$57 = 69 = 9$$

$$57 \overline{) 621} 10 \text{ £}$$

$$57 \overline{) 1020} 17 \text{ £}$$

$$\begin{array}{r} 51 \\ 20 \\ \hline 450 \\ 399 \\ \hline 51 \end{array}$$

$$57 \overline{) 612} 10 \text{ £}$$

$$57 \overline{) 168} 2 \text{ £}$$

5th If 9 cwt of sugar

cost 45 £ 2s 4d.

what is that per cwt

$$9 = 45 - 2 - 4 - 1$$

$$9 \overline{) 10828} 1355 \text{ (100)} \quad \begin{array}{r} 902 \quad 12 \quad 20 \\ 12 \quad 12 \quad 12 \\ \hline 28 \quad 15 \quad 12 \\ 24 \quad 12 \quad 33 \\ \hline 42 \quad 24 \quad 9 \end{array}$$

$$9 \overline{) 16} 2 \text{ £ } 0 \text{ s } 2 \text{ d}$$

Ans 5 = 12/9 1/2

6th If my income be 109 guineas per annum I desire to know what I may spend per day so that I may lay up 45 £

flowers

$$\begin{array}{r} \text{Days} \quad \text{£ } 0 \quad \text{Day} \\ 365 = 109 = 12 = 1 \end{array}$$

$$365 \overline{) 2152} 5$$

Answer 5 1/3 1/4

$$\begin{array}{r} 109 \\ 28 \\ \hline 472 \\ 218 \\ \hline 210 \end{array}$$

$$\begin{array}{r} 365 \overline{) 3924} 1 \\ 365 \\ \hline 274 \\ 4 \\ \hline 365 \overline{) 1096} 3 \\ 1095 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 210 \overline{) 3052} \\ 152 = 12 \\ 45 - 0 \\ \hline 109 = 12 \end{array}$$

Continued

7th If my salary be 43 £ 12¹/₅ per annum what does it

amount to per week

$$\text{Days } 365 - 43 = 12 = 5 = 7$$

$$\text{Answer } 1608 \text{ } 37 \text{ } 365$$

$$\begin{array}{r} 365 \overline{) 10489} \quad 12 \quad 11 \\ 730 \\ \hline 283 \\ 4 \\ \hline 1132 \quad 3 \\ 1095 \\ \hline 37 \end{array}$$

If my income be 169
 803 2 87 per week
 what is that per annum

$$\begin{array}{r} \text{Days } 7 = 14 = 8 = 3 \frac{37}{365} = 865 \\ 12 \\ 40 \\ 16 \\ \hline 200 \\ 4 \\ \hline 808 + 37 \\ 865 \end{array}$$

$$\begin{array}{r} 7 \overline{) 293132} \quad 41876 \quad 12 \\ 28 \\ \hline 13 \\ 7 \\ \hline 61 \\ 56 \\ \hline 53 \\ 49 \\ \hline 42 \\ 42 \\ \hline \end{array}$$

$$\begin{array}{r} 4 \overline{) 1876} \quad 469 \quad 12 \\ 16 \\ \hline 27 \\ 24 \\ \hline 36 \\ 36 \\ \hline \end{array}$$

$$\begin{array}{r} 20 \overline{) 852432} \\ 80 \\ \hline 52 \\ 40 \\ \hline 128 \end{array}$$

Answer 43 £ 12¹/₅ 2 11

Continued

9th If I am to pay 1st per week for pasturing
 And what must I give for 37 cows

can I do work

$$1 = 1 - 2 - 37$$

$$\frac{12}{19}$$

$$\frac{19}{37}$$

$$\frac{37}{133}$$

$$\frac{133}{57} 20$$

$$12 \overline{) 903} (58(2$$

$$\frac{60}{103} \frac{40}{18}$$

$$\frac{94}{9}$$

Ans 2 18 57

How many yards of cloth may
 be bought for 57 £ 13
 when 9 1/2 yds. 9 £ 15 5 1/2

£ 5 2 2 2 2 2 2 2

$$9 = 15 = 5 = 2 = 9 \frac{1}{2} = 57 = 13$$

$$\frac{20}{75}$$

$$\frac{75}{12}$$

$$\frac{12}{905}$$

$$\frac{905}{4}$$

$$\frac{4}{3622}$$

$$\frac{2}{19}$$

$$\frac{19}{1153}$$

$$\frac{1153}{12}$$

$$\frac{12}{13836}$$

$$\frac{13836}{4}$$

$$\frac{4}{55344}$$

$$\frac{55344}{19}$$

$$\frac{19}{498096}$$

$$\frac{498096}{55344}$$

$$3622 \overline{) 1051536} (290(145$$

$$\frac{7244}{32713}$$

$$\frac{32713}{32598}$$

$$\frac{32598}{1156}$$

$$\frac{1156}{2}$$

$$\frac{2}{2312}$$

$$\frac{2312}{4}$$

$$3622 \overline{) 9248} (2$$

$$\frac{7244}{2004}$$

$$\frac{2004}{3622}$$

$$\frac{3622}{2004}$$

$$\frac{2004}{3622}$$

$$\frac{3622}{2004}$$

Answers 145 yds 290 2004 3622

Continued

25

11th I sold a vessel for 15000 Dollars and Town's
 $\frac{5}{16}$ what was my part of the money

$$\begin{array}{r}
 16 = 25000 = 5 \\
 \hline
 16 \overline{) 125000} (781 \\
 \underline{112} \\
 130 \\
 \underline{128} \\
 20 \\
 \underline{16} \\
 400 (25 \\
 \underline{32} \\
 80 \\
 \underline{80} \\
 0
 \end{array}$$

Ans. 781 $\frac{1}{5}$ 25 sh

12th The united states pay 6 per cent Interest on part
of their Domestic Debt and supposing they
could borrow money in Holland for 3 1/2 per cent
how much would they gain annually
by borrowing 5 millions of Dollars in Holland
and applying to the payment of said debt

$$\begin{array}{r}
 \text{Dollars} \\
 2 \overline{) 1000000} \\
 \underline{2000000} \\
 5000000 \\
 \underline{2500000} \\
 2500000
 \end{array}$$

Ans. 25000 Dollars



Continued

A gentleman sent a ship on a whaling voyage
and agreed to divide the proceeds of the voyage into 60 shares
and give the captain of the ship afterwards returned with
a cargo worth 10 thousand Dollars a demand the
captain should

Share Sol Share
40 - 10000 = 1

Sol
165 = 656 $\frac{2}{3}$

610 / 10.000 / 60

665 = 656 $\frac{2}{3}$

40
36
40
36
6 / 400 (66

Sol of miller
Share 665 = 656 $\frac{2}{3}$

40
36
6 / 400 (6
36
2 / 4.2
5.3

1/10 A merchant in Connecticut paid a merchant in
England £4349 14s 6d in Dollars at 47/6 each
how much was that valued at in new england
currency

£ 4 - 6 = 6 = 4349 = 16 = 4
12
54

86996
12
173996
86996
1043956
54 / 6263736 (115995
54
86
323
290
517
486
513
486
236
230
6
54 / 115995
54
6 / 115995

Answer £ 3799 15
21/3

Continued

27

15th Q1 How much must you give for A keg of cider containing
 7 1/2 gallons at the rate of 2 Dollars per barrel

$$\begin{array}{r} \text{gal} \quad \text{Dol} \quad \text{gal} \\ 7\frac{1}{2} - 2 = 5\frac{1}{2} \\ \underline{2} \quad \underline{15} \\ 63 \end{array}$$

$$\begin{array}{r} 63 \overline{) 30.00} (47 \quad \text{Ans } 47 \text{ cents } 6 \text{ mills } \frac{12}{63} \\ \underline{252} \\ 480 \\ \underline{441} \\ 390 \\ \underline{378} \\ 12 \\ \underline{63} \end{array}$$

16th Suppose you have 476 Dollars 37 cents of paper stock
 and every Dollar is worth 65 cents how much is the
 whole worth

$$\begin{array}{r} \text{Dol} \quad \text{Cts} \quad \text{Dol} \quad \text{Cts} \\ 100 - 65 = 476 - 37 \\ \quad \quad \quad 65 \end{array}$$

$$\begin{array}{r} 2381 = 85 \\ 28582 = 2 \end{array}$$

$$\begin{array}{r} 100 \overline{) 30964} = 65 (309/64 \quad \text{Ans } 309 \text{ Dol } 64 \text{ Cts} \\ \underline{300} \\ 964 \\ \underline{900} \\ 640 \\ \underline{600} \\ 404 \\ \underline{400} \\ 4 \end{array}$$

Continued

17th Harry had apples of which were worth 6
 Billy had pears 8 of which were worth 2
 I demand how many pears Billy must give Harry
 Harry had pears 9 of which were worth 6
 Billy had apples 8 of which were worth 2
 I demand what number of apples Billy must
 give Harry for 15 of his pears

Pears I Pears

$$9 = 6 = 15$$

$$\begin{array}{r} 2 \overline{) 90} (10 \text{ Ans} \\ \underline{20} \end{array}$$

I Apples I

$$2 = 8 = 10$$

$$\begin{array}{r} 2 \overline{) 80} (40 \text{ Ans} \\ \underline{40} \end{array}$$

Answer 40 Apples

18th A man bought a piece of cloth 9 quarters wide
 and 11 quarters long how many yards of $\frac{3}{4}$
 cloth will line it

qr qr qr

$$\text{Ans } 3 = 11 = 9$$

$$\begin{array}{r} 3 \overline{) 99} (33 \text{ Ans} \\ \underline{99} \\ 0 \end{array}$$

$$\begin{array}{r} 4 \overline{) 32} (8 \\ \underline{32} \\ 0 \end{array}$$

Answer 8 yards $\frac{1}{4}$



Continued

29

14th I said Harry to sick my purse and money are worth 3 1/4 guineas but the money is worth 11 times as much as the purse pray how much money is there in it.

Part guineas Part

$$12 - 3 = 9 = 1$$

$$\frac{28}{31}$$

$$12 \overline{) 91} (7$$

$$12 \overline{) 84} (7$$

$$L_4 = 3 = 5 \text{ Answer}$$

20th If my horse and saddle are worth 18 guineas and my horse be worth 5 times as much as my saddle pray what is the value of my horse.

Part guineas Part

$$18 - 3 = 15 = 1$$

$$\frac{28}{144}$$

$$7 \overline{) 504} (72$$

$$6 \overline{) 432} (72 \text{ Dollars}$$

Continued

21st *Q* is A cistern being 4 cocks the first will empty it in 10 minutes the second in 20 the third in 40 the fourth in 80 minutes in what time will all four running together empty it

Time	times
10	6
20	3
40	1 1/2
80	3/4
	<u>11 3/4</u>

in 60 minutes

cistern Min cistern

$$\frac{11 \frac{3}{4} = 60 - \frac{1}{4}}{\frac{4}{45} \overline{) 240} \left| \frac{1}{5} \right.}$$

$\frac{15}{45} \frac{1}{3}$ Ans $5 \frac{1}{3}$ minutes

22nd *Q* and *B* depart from the same place and travel the same road but *A* goes 5 days before *B* at the rate of 20 miles per day *B* follows at the rate of 25 miles per day

In what time will the distance will be over

Miles	Days	Miles	Days
25	1 = 20 = 5		
20	<u>5</u>		
5	100		

Miles	Days	Miles
5 = 1 - 200		

$$5 \overline{) 100} \left(20 \text{ Days Ans} \right)$$

Miles	Days
1 = 25 - 20	
20	
1/500 (500 Miles Ans	
500	

Continued

23rd I can do a piece of work in 3 weeks I can do
 three as much in 9 weeks and 6 5 times as
 much in 12 weeks in what time can
 they do it jointly

Jobs

I can do the job 5 times in 12 weeks

3rd Job
 $3 = 1 - 12$
 $3 \overline{) 12} \begin{matrix} 4 \\ 12 \end{matrix}$

Job	Weeks	Job
$13 \frac{1}{2}$	$\frac{12}{2}$	$\frac{1}{2}$
$\frac{2}{27}$	$\frac{2}{24}$	$\frac{2}{2}$

$9 = 3 = 12$
 $9 \overline{) 36} \begin{matrix} 4 \\ 36 \end{matrix}$
 $4 \frac{1}{2}$

$29 \overline{) 144} \begin{matrix} 5 \\ 135 \\ 9 \end{matrix}$ Answer 5 Days 4 hours
 $29 \overline{) 108} \begin{matrix} 4 \\ 108 \end{matrix}$

Note in the above sum 6 days
 is called a week 12 hours a day

24th The hour and minute hand of a clock
 are exactly together at 12 o'clock when
 are they next together

$11 = 1 - 12$
 $11 \overline{) 12} \begin{matrix} 1 \text{ hour} \\ 11 \end{matrix}$ Ans 1 hour 55 min
 $11 \overline{) 60} \begin{matrix} 5 \text{ min} \\ 55 \end{matrix}$

C. Method

of assessing towns on personal taxes

1st An inventory of the value of all the estates both real and the number of polls for which each person is rateable must be taken in separate columns. Then to know then to know what must be paid on the dollar make the total value of the inventory. The first town the town to be assessed the second and third the third and the quotient will show the value on the dollar

2nd Make a table by multiplying the value on the dollar by 1, 2, 3, 4, 5 &c

3rd From the inventory take the real and personal estates of each man and find them separately in the table which will will show you man's proportional share of the tax for real and personal estates

If any part of the tax be averaged on the polls before stating to find the value on the dollar deduct the sum of the average tax from the whole sum to be assessed for which average make a separate column as well as for the real and personal estates

Example

Suppose the general court should grant a tax of 25,000 dollars of which a certain

Continued

town is to pay 5000 for road and of which the place
 being 624 one to pay 75 cents each the towns inventory
 is 69568 dollars what will it be on the dollar and
 what is it tax as by the inventory where what is

of follow we need 856 dollars personal 1000 dollars and he has
 4 polls

$$\begin{array}{r}
 1 = 75 - 624 \\
 \quad 75 \\
 \hline
 3120 \\
 4568 \\
 \hline
 4680
 \end{array}$$

69568 = 2782-72-1

69568 / 2782-72 / 4 cents on the dollar

1	2	3	4	5	6	7	8	9	10
1	2	3	4	5	6	7	8	9	10
1	2	3	4	5	6	7	8	9	10
1	2	3	4	5	6	7	8	9	10
1	2	3	4	5	6	7	8	9	10
1	2	3	4	5	6	7	8	9	10
1	2	3	4	5	6	7	8	9	10
1	2	3	4	5	6	7	8	9	10
1	2	3	4	5	6	7	8	9	10
1	2	3	4	5	6	7	8	9	10

Now to find what his rate is
 his real estate being 856 I find
 by the table that 856 is 52 dollars

that 50
 real estate 54 24
 personal 3 00
 polls 75 41 36
 300

Real Estate	Personal	Polls	Total
54 24	3 00	41 36	98 60

34 Rule of Three Inverse

Examples

1st Suppose I lend my friend 350 £ for 5 months he promising the like kindness but when requested I can have but 125 £ how long may I keep it to balance the favour

$$\begin{array}{r}
 \text{£} \quad \text{Months} \quad \text{£} \\
 350 = 5 = 125 \\
 125 \overline{) 1750} \quad (14 \text{ Months Answer} \\
 \underline{125} \\
 500
 \end{array}$$

2nd Suppose 450 men are in a garrison and their provisions are calculated to last but 5 months how many must leave the garrison that the same provisions may be sufficient for those who remain 9 months

$$\begin{array}{r}
 \text{Months} \quad \text{Men} \quad \text{Months} \\
 5 = 450 = 9 \\
 9 \overline{) 2250} \quad (250 \\
 \underline{18} \\
 45 \\
 \underline{45} \\
 0
 \end{array}$$

$$\begin{array}{r}
 250 - 450 \\
 \underline{250} \\
 200
 \end{array}$$

Answer 200

Continued

35

If A man perform a Journey in 15 days
when the way is 12 hours long in how many
will he do it when the day is but 10 hours
long.

$$\begin{array}{r}
 \text{hours} \quad \text{Days} \quad \text{hours} \\
 12 = 15 = 10 \\
 \quad \quad 12 \\
 \quad \quad \underline{30} \\
 10 \overline{) 150} \quad 15 \text{ Days Answer} \\
 \quad \underline{10} \\
 \quad \quad 50 \\
 \quad \quad \underline{50} \\
 \quad \quad \quad 0
 \end{array}$$

What number of men must be
employed to finish it in 9 days what 15
men would be 30 days about

$$\begin{array}{r}
 \text{Days} \quad \text{Men} \quad \text{Days} \\
 30 = 15 = 9 \\
 \quad \quad 30 \\
 9 \overline{) 450} \quad 50 \text{ Men Ans} \\
 \quad \underline{45} \\
 \quad \quad 0
 \end{array}$$

If a field will feed 6 cows 90 days
how long will it feed 21 cows

$$\begin{array}{r}
 \text{cows} \quad \text{Days} \quad \text{cows} \\
 6 = 90 = 21 \\
 \quad \quad 6 \\
 21 \overline{) 540} \quad 26 \text{ Days Answer} \\
 \quad \underline{42} \\
 \quad \quad 120 \\
 \quad \quad \underline{120} \\
 \quad \quad \quad 0
 \end{array}$$

Double Rule of Three

Examples

If 100 £ gain 6 £ in 1 year what will
400 £ gain in 9 months

$$\begin{array}{rcl} \text{£} & \text{Month} & \text{£ Interest} \\ 100 & = 12 & = 6 \\ 400 & = 9 & = \end{array}$$

$$\frac{3600}{9}$$

$$\frac{100}{12} \text{ Divisor}$$

$$12/00 \overline{) 21600} 18 \text{ Answer}$$

If 400 £ gain 18 £ in 9 months what
is the rate per cent per annum

$$\begin{array}{rcl} \text{£} & \text{M} & \text{£} \\ 400 & = 9 & = 18 \\ 100 & = 12 & = \end{array}$$

$$\frac{400}{9}$$

$$\frac{1200}{18}$$

$$\frac{9600}{1200}$$

$$36/00 \overline{) 21600} 6 \text{ Answer}$$

What principal at 6 per cent per
annum will gain 18 £ in 9 months

$$\begin{array}{rcl} \text{£} & \text{M} & \text{£} \\ 100 & = 12 & = 6 \\ 12 & = 9 & = 18 \end{array}$$

$$\frac{9}{6}$$

$$\frac{1200}{18}$$

$$\frac{9600}{1200}$$

$$54 \overline{) 21600} 400 \text{ Answer}$$

Continued

37

If 8 men spend 32 £ in 13 weeks what
will 24 men spend in 52 weeks

Men Weeks £

$$8 = 13 = 32$$

$$24 = 52$$

32	13
104	8
156	104
1664	
24	
6656	

\$328

104 | 3328 (384 Answer

312
 816
 832
 416
 416

If the freight of 9 lbs of sugar each weighing
12 cwt 20 bagues cost 16 £ what must
be paid for the freight of 50 tierces each
weighing 2½ cwt 100 bagues

lbs bagues £

$$9 = 20 = 16$$

2160	200
2½	125
100	500
125	200
125	100

9
12
108
20
2160

12500
12516
75000
12500

2140 | 20000 (092 128 Answer

1944
 560
 432
 128

Continued

There was Aester's edifice completed in
 A year by 20 workmen but the same
 being demolished it is ~~necessary~~
 necessary that just such another
 should be built in 5 months & I demand
 the number of men to be employed
 about it

Men Men the edifice

$$\begin{array}{r}
 20 = 12 = 1 \\
 12 \quad 5 = 1 \\
 5 \overline{) 240} (48 \\
 \underline{20} \\
 40 \\
 \underline{40} \\
 0
 \end{array}$$

48 Men Answer

If 6 men build A wall 20 feet long
 6 feet high and 4 ft thick in
 16 days in what time will 24 men
 build one 200 ft long 8 ft high and 6 ft thick

Men Day

$$\begin{array}{r}
 6 = 16 = 20 \times 6 \times 4 \\
 24 = \dots - 200 \times 8 \times 6 \\
 \underline{480} \quad \underline{48} \\
 1920 \quad 1600 \\
 \underline{96} \quad \underline{800} \\
 11520 \quad 9600 \\
 \quad \quad \underline{16} \\
 \quad \quad 57600 \\
 \quad \quad \underline{9600} \\
 \quad \quad 153600 \\
 \quad \quad \underline{6} \\
 11520 / 921600 (80 Days Answer
 \end{array}$$

29

Vulgar Fractions

Examples

What is the greatest common measure of 1836
 $3996 = 1044$

$$1836/3996(2$$

$$\begin{array}{r} 3672 \\ \underline{1836} \\ 1836 \end{array}$$

$$1836/5$$

$$\begin{array}{r} 1820 \\ \underline{16} \\ 216 \end{array}$$

$$324/1$$

$$\begin{array}{r} 216 \\ \underline{216} \\ 0 \end{array}$$

$$108/1044/9$$

$$\begin{array}{r} 972 \\ \underline{972} \\ 0 \end{array}$$

$$72/108/2$$

$$\begin{array}{r} 72 \\ \underline{72} \\ 0 \end{array}$$

$$36/72/2$$

$$\begin{array}{r} 72 \\ \underline{72} \\ 0 \end{array}$$

36 the answer required

What is the greatest common measure of
 $1224 = \text{and } 1080$

$$1080/1224(1$$

$$\begin{array}{r} 1080 \\ \underline{1080} \\ 0 \end{array}$$

$$144/1080(7$$

$$\begin{array}{r} 1008 \\ \underline{1008} \\ 0 \end{array}$$

$$72/144(2 \text{ Answer } 72$$

$$\begin{array}{r} 144 \\ \underline{144} \\ 0 \end{array}$$

Problem 2nd

Examples

What is the least common multiple of
 $10 - 16 \text{ and } 20$

$$\begin{array}{r} 4 \\ \underline{5} \\ 20 \end{array} \quad \begin{array}{r} 40 \\ \underline{3} \\ 120 \end{array} \quad \begin{array}{r} 40 \\ \underline{2} \\ 240 \end{array} \text{ Ans}$$

$$4 \mid 6 = 10 = 16 = 20$$

$$5 \mid 6 = 10 = 4 = 5$$

$$2 \mid 6 = 2 = 4 = 1$$

$$3 = 1 = 2 = 1$$

Continued

What is the least common multiple of 6 and 8

$$\begin{array}{r} 2 \\ 3 \\ \hline 6 \\ 4 \\ \hline 12 \end{array} \text{ Ans}$$

$$\frac{2}{3} = \frac{8}{4}$$

What is the least number

3-5-8 and 10 will measure

$$\begin{array}{r} 5 \\ 2 \\ \hline 10 \\ 3 \\ \hline 30 \\ 4 \\ \hline 120 \end{array} \text{ Answer}$$

$$\begin{array}{r|l} 3-5-8-10 & \\ 3-1-8-2 & \\ 3-1-4-1 & \end{array}$$

What is the least number which can be divided by the 9 digits separately without remainder

$$\begin{array}{r|l} 3 & 123456789 \\ 2 & 121452783 \\ 2 & 111251743 \\ 2 & 111151723 \end{array}$$

$$\begin{array}{r} 3 \\ 2 \\ \hline 6 \\ 2 \\ \hline 12 \\ 5 \\ \hline 60 \\ 7 \\ \hline 420 \\ 2 \\ \hline 840 \\ 3 \\ \hline 2520 \end{array} \text{ Answer}$$

Reduction of Vulgar Fractions

Examples

Reduce $\frac{288}{480}$ to its lowest terms

$$\frac{288}{480} = \frac{36}{60} = \frac{6}{10} = \frac{3}{5} \text{ Answer}$$

Reduce $\frac{57}{456}$ to its lowest terms

$$\frac{57}{456} = \frac{1}{8} \text{ Answer}$$

Reduce $\frac{1429}{2858}$ to its lowest terms

$$\frac{1429}{2858} = \frac{1}{2} \text{ Answer}$$

Case 2nd

Examples

To reduce a mixed number to its equivalent improper fraction

Reduce $36\frac{5}{8}$ to its equivalent improper fraction

$$36\frac{5}{8} = \frac{293}{8} \text{ Answer}$$

Continued

Reduce $653\frac{3}{19}$ to its equivalent improper fraction.

$$\begin{array}{r} 653\frac{3}{19} \\ 19 \overline{) 5880} \\ \underline{653} \\ 12410 \end{array}$$

$$\frac{12410}{19} \text{ Answer}$$

Case 3rd

To reduce A whole number to an equivalent fraction having A given denominator

Examples

Reduce 6 to A fraction whose denominator shall be 8

$$\frac{8}{8} \quad \frac{48}{8} \text{ Ans}$$

Case 4th

To reduce an improper fraction to its equivalent whole or mixed number

Examples

Reduce $\frac{293}{8}$ to its equivalent whole or mixed number

$$\frac{8 \overline{) 293}}{36\frac{5}{8}} \text{ Answer}$$

Case 5th

To reduce a compound fraction to an equivalent one

Examples

Reduce $\frac{1}{2}$ of $\frac{2}{3}$ of $\frac{3}{4}$ of $\frac{4}{5}$ to a simple fraction

$$\begin{array}{r} \frac{1}{2} \text{ of } \frac{2}{3} \text{ of } \frac{3}{4} \text{ of } \frac{4}{5} \\ \frac{1}{2} \times \frac{2}{3} \times \frac{3}{4} \times \frac{4}{5} = \frac{1 \times 2 \times 3 \times 4}{2 \times 3 \times 4 \times 5} = \frac{24}{120} = \frac{1}{5} \end{array}$$

Reduce $\frac{3}{4}$ of $\frac{4}{5}$ of $\frac{5}{6}$ of $1\frac{1}{2}$ to a simple fraction

$$\begin{array}{r} \frac{3}{4} \text{ of } \frac{4}{5} \text{ of } \frac{5}{6} \text{ of } 1\frac{1}{2} \\ \frac{3}{4} \times \frac{4}{5} \times \frac{5}{6} \times \frac{3}{2} = \frac{3 \times 4 \times 5 \times 3}{4 \times 5 \times 6 \times 2} = \frac{180}{240} = \frac{3}{4} \end{array}$$

Case 6th

To find the value of a fraction in the known parts of the integer or of coin weight measure &c

Examples

Case 6th

To reduce fractions of different denominators to equivalent fractions having a common denominator

Examples

Reduce $\frac{1}{4}$, $\frac{2}{5}$ and $\frac{5}{8}$ to equivalent fractions having a common denominator

$\frac{1}{4}$	$\frac{2}{5}$	$\frac{5}{8}$	
$\frac{2}{8}$	$\frac{4}{10}$	$\frac{5}{8}$	
$\frac{5}{16}$	$\frac{8}{20}$	$\frac{10}{16}$	
$\frac{10}{32}$	$\frac{16}{40}$	$\frac{20}{32}$	
$\frac{25}{80}$	$\frac{40}{80}$	$\frac{50}{80}$	

$\frac{40 = 64}{160} \quad \frac{100}{160} \quad \text{Common}$

Reduce $\frac{1}{2}$, $\frac{2}{3}$, $\frac{3}{4}$, $\frac{5}{6}$ and $\frac{7}{8}$ to fractions having a common denominator

1	2	3	5	7	
2	3	4	6	8	
2	4	5	18		
4	4	20	18		
4	12	160	144		
16	6	3	3		
96	72	480	482		
8	8	2	2		
768	576	960	864		
				7	
				6	
				42	
				4	
				168	
				3	
				504	
				2	
				1008	
					8
					6
					48
					4
					192
					3
					576
					2

1) Rule 2nd

45

To reduce any given fractions to others which shall have the least common denominator

Examples

Reduce $\frac{1}{3}$ $\frac{3}{4}$ and $\frac{7}{8}$ to fractions having the least common denominator

$$\begin{array}{r|rrr} 4 & 1 & 3 & 7 \\ \hline 3 & 3 & 4 & 8 \\ \hline 12 & 3 & 1 & 2 \end{array}$$

$$\frac{1}{3} \times \frac{8}{8} = \frac{8}{24}$$

$$\frac{3}{4} \times \frac{3}{3} = \frac{9}{12}$$

Answer

Case 3rd

To reduce a fraction of one denominator to the fraction of another but greater retaining the same value

Examples

Reduce $\frac{3}{5}$ of penny to the fraction of a pound

$$\begin{array}{r|rr} 5 & 3 & 1 \\ \hline 5 & 12 & 20 \\ \hline & 60 & 20 \\ \hline & 1200 & \end{array}$$

$$3 \frac{1}{4} \times \frac{1}{4} = \frac{1}{4}$$

Answer

Continued

Reduce $\frac{3}{4}$ of farthing to the fraction of
A pound

$$\begin{array}{r} \frac{3}{4} \quad \frac{1}{4} \quad \frac{1}{12} \quad \frac{1}{20} \\ 3840 \quad 1280 \end{array} \text{ Answer}$$

$$\begin{array}{r} 3840 \\ 160 \\ 12 \\ 192 \\ 20 \\ 3840 \end{array}$$

Reduce $\frac{5}{8}$ of A penny to the fraction of A
guinea

$$\begin{array}{r} \frac{5}{8} \quad \frac{1}{12} \quad \frac{1}{28} \\ 2688 \end{array} \text{ Answer}$$

$$\begin{array}{r} 2688 \\ 560 \\ 28 \\ 568 \\ 192 \\ 2688 \end{array}$$

Reduce $\frac{1}{4}$ of A shilling to the fraction
of moidore

$$\begin{array}{r} \frac{12}{19} \quad \frac{1}{36} \\ 684 \quad 114 \quad 39 \end{array} \text{ Answer}$$

$$\begin{array}{r} 684 \\ 19 \\ 324 \\ 36 \\ 684 \end{array}$$

Reduce $\frac{4}{5}$ of an ounce to the fraction of A
livre

$$\begin{array}{r} \frac{4}{7} \quad \frac{1}{16} \\ 112 \end{array}$$

$$\begin{array}{r} \frac{4}{7} \quad \frac{1}{12} \quad \frac{1}{28} \end{array} \text{ Answer}$$

Continued

47

Reduce $\frac{3}{4}$ to the fraction of 12

$$\frac{3}{4} = \frac{9}{12}$$

$$\frac{42}{1} \quad \frac{1}{12} \quad \frac{1}{20}$$

$$\frac{240}{6} \quad \frac{42}{7} \quad \frac{40}{40} \text{ Answer}$$

Reduce $\frac{13}{16}$ to the fraction of 16

$$\frac{13}{16} = \frac{13}{16}$$

$$\frac{162}{1} \quad \frac{1}{12} \quad \frac{1}{22}$$

$$\frac{264}{3} \quad \frac{162}{54} \quad \frac{2}{88} = 44 \text{ Answer}$$

Reduce $\frac{4}{5}$ of a pound to the fraction of 1

Answer

$$\frac{4}{5} \quad \frac{20}{1} \quad \frac{1}{28}$$

$$\frac{28}{80} \quad \frac{10}{140} \quad \frac{2}{8} \quad \frac{4}{4} \text{ Answer}$$

Reduce $\frac{7}{8}$ of 12 to the fraction of 1

Answer

$$\frac{7}{8} \quad \frac{1}{20} \quad \frac{1}{12}$$

$$\frac{7}{1920} \text{ Answer}$$

Reduce $\frac{8}{9}$ of 12 to the fraction of 1

Answer

$$\frac{8}{9} \quad \frac{1}{28} \quad \frac{1}{4}$$

$$\frac{252}{1008} \quad \frac{8}{1008} \quad \frac{1}{126} \text{ Answer}$$

Continued

Reduce $\frac{1}{4}$ of A farthing to the fraction
of A shilling

$$\begin{array}{r} 1 \\ 4 \\ \hline 1 \\ 4 \\ \hline 1 \\ 12 \\ 4 \\ \hline 28 \\ 4 \\ \hline 192 \end{array}$$

$\frac{1}{192}$ Ans

Case 4 $\frac{11}{11}$

To reduce A fraction of one denominator to the fraction of another but keep retaining the same value

Examples

Reduce $\frac{1}{400}$ of A L to the fractions of A penny

$$\begin{array}{r}
 12 \quad 4 \quad 2 \\
 20 \quad 12 \\
 \hline
 400 \quad 1 \quad 1 \quad 10 \quad 240 \quad 24 \quad 6 \quad 3 \\
 \hline
 400 \quad 40 \quad 10 \quad 5
 \end{array}
 \text{ Answer}$$

Reduce $\frac{1}{1280}$ of A pound to the fractions
of A farthing

1	20	12	4
1240	1	7	1

20				
12				
240	4		4	
4				
250	44	12		3
1200	128	16		4

五

$\begin{array}{r} 9 \overline{) 1680} \\ 2688 \\ \hline \end{array}$	$\begin{array}{r} 6 \\ 210 \\ \hline 336 \end{array}$	$\begin{array}{r} 7 \\ 35 \\ \hline 56 \end{array}$	$\begin{array}{r} 5 \\ 8 \\ \hline \end{array}$	Answer	$\begin{array}{r} 56 \\ 28 \\ \hline 336 \\ 5 \\ \hline 1680 \end{array}$
--	---	---	---	--------	---

Reduce $\frac{1}{57}$ of a mile to the fraction of
A shilling

$$\begin{array}{r} 1 \quad 36 \\ - 57 \quad 1 \\ \hline \end{array}$$
$$\begin{array}{r} 3 \quad 36 \quad 12 \\ - 57 \quad 19 \\ \hline \end{array} \text{Answer}$$

$$\begin{array}{r} 4 \overline{) 28} \\ 7 \overline{) 1} \end{array}$$

$$\begin{array}{r} 28 \\ 4 \\ 7 \overline{) 20} \\ 140 \end{array}$$

$$\begin{array}{r} 28 \\ 4 \\ 7 \overline{) 20} \\ 140 \end{array}$$

$$\begin{array}{r} 7 \\ 8 \\ 10 \end{array}$$

$$\begin{array}{r} 2 \\ 4 \\ 5 \end{array}$$

$$\begin{array}{r} 7 \\ 1920 \\ \hline 12 \\ 1 \\ \hline 20 \\ 1 \\ \hline 20 \\ 12 \\ \hline 240 \\ 7 \\ \hline 1680 \end{array}$$

		6	5	
\$	1550	210	35	17
	<u>1920</u>	<u>240</u>	<u>40</u>	<u>5</u>

28 Nov

Continued

Reduce $\frac{1}{126}$ of A into $\frac{1}{10}$ the fraction of
A the Swindon is

$$\begin{array}{r} 1 \quad 112 \\ 126 \quad 1 \end{array} \quad \begin{array}{r} 7 \quad 112 \quad 16 \\ 126 \quad 18 \end{array} \quad \begin{array}{r} 8 \quad 112 \\ 9 \end{array} \quad \text{Answer}$$

Case 3rd.

To find the value of A fraction in the
known part of the integer as of coins
weight measure &c

Examples

What is the value of $\frac{5}{7}$ of A pound

$$\begin{array}{r} 5 \\ 7 \overline{) 100} (14 \\ \underline{7} \\ 30 \\ \underline{28} \\ 2 \\ \underline{12} \\ 7 \overline{) 24} (3 \\ \underline{21} \\ 3 \\ \underline{4} \\ 7 \overline{) 12} (1 \\ \underline{7} \\ 5 \\ \underline{7} \end{array}$$

Answer $14 = 3 = 1 \frac{5}{7}$

What is the value of $\frac{9}{24}$ of A shilling

$$\begin{array}{r} 9 \\ 24 \overline{) 108} (4 \\ \underline{96} \\ 12 \\ \underline{12} \\ 0 \end{array}$$

Ans $4 \frac{1}{2}$

What is the value of $\frac{17}{29}$ of A new £

$$\begin{array}{r} 17 \\ 29 \overline{) 68} (2 \\ \underline{58} \\ 10 \\ \underline{28} \\ 80 \\ \underline{58} \\ 220 \\ \underline{261} \\ 19 \\ \underline{28} \\ 114 \\ \underline{114} \\ 0 \end{array}$$

$$\begin{array}{r} 17 \\ 29 \overline{) 304} (10 \\ \underline{29} \\ 14 \\ \underline{15} \\ 84 \\ \underline{84} \\ 0 \end{array}$$

Ans $2 \text{ gr } 9 \text{ th } 2$
 $\frac{21}{29}$

Continued

What is the value of $\frac{4}{5}$ of a pound hundred p's

$$\begin{array}{r} 4 \\ 16 \\ 5 \overline{) 64} (12 \\ \underline{50} \\ 14 \\ \underline{10} \\ 4 \\ 16 \\ 5 \overline{) 64} (12 \\ \underline{50} \\ 14 \\ \underline{10} \\ 4 \\ \underline{5} \end{array}$$

Answer

What is the value of $\frac{3}{5}$ of a lb Troy

$$\begin{array}{r} 3 \\ 12 \\ 5 \overline{) 36} (7 \\ \underline{35} \\ 1 \\ 20 \\ 5 \overline{) 20} (4 \\ \underline{20} \end{array}$$

7 lb 4 part Answer

What is the value of $\frac{1}{13}$ of a ton

$$\begin{array}{r} 3 \\ 20 \\ 13 \overline{) 60} (4 \\ \underline{52} \\ 8 \\ 112 \\ 13 \overline{) 996} (68 \\ \underline{78} \\ 116 \\ \underline{104} \\ 12 \\ 16 \\ \underline{13} \\ 3 \\ 122 \\ 13 \overline{) 192} (14 \\ \underline{182} \\ 10 \\ 116 \\ 13 \overline{) 160} (12 \\ \underline{156} \\ 4 \\ 52 \\ \underline{52} \\ 0 \\ 10 \\ 16 \\ 13 \overline{) 160} (12 \\ \underline{156} \\ 4 \\ 52 \\ \underline{52} \\ 0 \\ 10 \\ 16 \\ 13 \overline{) 160} (12 \\ \underline{156} \\ 4 \end{array}$$

Answer 4 cent 68 lb
14 lb 12 $\frac{4}{13}$ Answer

Continued

What is the value $\frac{6}{5}$ of A year

$$\begin{array}{r} 6 \\ 5 \overline{) 24} 4 \\ \underline{18} \end{array}$$

$$\begin{array}{r} 6 \\ 5 \overline{) 24} 4 \\ \underline{18} \end{array}$$

$$\begin{array}{r} 6 \\ 5 \overline{) 24} 4 \\ \underline{18} \\ 3 \overline{) 16} 5 \end{array}$$

Ans 2 yr 23. 1/3

What is the value of $\frac{7}{8}$ of an ell englis

$$\begin{array}{r} 7 \\ 8 \overline{) 35} 4 \\ \underline{32} \\ 3 \end{array}$$

Ans 4 yr 1 1/2

$$\begin{array}{r} 7 \\ 8 \overline{) 35} 4 \\ \underline{32} \\ 3 \end{array}$$

$$\begin{array}{r} 7 \\ 8 \overline{) 35} 4 \\ \underline{32} \\ 3 \end{array}$$

What is the value of $\frac{9}{13}$ of A Day

$$\begin{array}{r} 9 \\ 13 \overline{) 24} 18 \\ \underline{13} \end{array}$$

$$\begin{array}{r} 9 \\ 13 \overline{) 24} 18 \\ \underline{13} \end{array}$$

$$\begin{array}{r} 9 \\ 13 \overline{) 24} 18 \\ \underline{13} \end{array}$$

$$\begin{array}{r} 9 \\ 13 \overline{) 24} 18 \\ \underline{13} \end{array}$$

$$\begin{array}{r} 9 \\ 13 \overline{) 24} 18 \\ \underline{13} \end{array}$$

$$\begin{array}{r} 9 \\ 13 \overline{) 24} 18 \\ \underline{13} \end{array}$$

$$\begin{array}{r} 9 \\ 13 \overline{) 24} 18 \\ \underline{13} \end{array}$$

$$\begin{array}{r} 9 \\ 13 \overline{) 24} 18 \\ \underline{13} \end{array}$$

Ans 16 hours
M
36-55 5/13

Continued

What is the value of $\frac{5}{8}$ of 4 mill.

$$\begin{array}{r} 5 \\ 8 \overline{) 40} 6 \\ 36 \\ \hline 4 \end{array}$$

$$\begin{array}{r} 4 \\ 6 \overline{) 160} 26 \\ 12 \\ \hline 40 \\ 36 \\ \hline 4 \end{array}$$

$$\begin{array}{r} 4 \\ 6 \overline{) 66} 11 \\ 6 \\ \hline 6 \end{array}$$

Cur. Arith. Ex.

6 26 11 Answer

What is the value of $\frac{3}{5}$ of 1000

$$\begin{array}{r} 3 \\ 5 \overline{) 108} 21 \\ 10 \\ \hline 8 \end{array}$$

$$\begin{array}{r} 8 \\ 5 \\ \hline 3 \\ 5 \overline{) 15} 3 \\ 15 \\ \hline 0 \end{array}$$

21 = $17\frac{1}{5}$ Answer

What is the value of $\frac{6}{7}$ of An Acre

$$\begin{array}{r} 6 \\ 7 \overline{) 24} 3 \\ 21 \\ \hline 3 \end{array}$$

$$\begin{array}{r} 40 \\ 7 \overline{) 120} 17 \\ 70 \\ \hline 50 \\ 49 \\ \hline 1 \end{array}$$

Answer 3 and $17\frac{1}{7}$ ptes

Case 10 $\frac{H}{I}$

To reduce any given quantity to the fraction of any greater denomination of the same kind

54

Continued

Examples

Reduce $14 \text{ } 3 \frac{1}{4} - \frac{5}{7}$ to the fraction of A pound

$$\begin{array}{r}
 20 \\
 12 \\
 \hline
 240 \\
 4 \\
 \hline
 960 \\
 7 \\
 \hline
 6720
 \end{array}
 \qquad
 \begin{array}{r}
 14 = 3 = 1 \frac{5}{7} \\
 12 \\
 \hline
 31 \\
 14 \\
 \hline
 171 \\
 4 \\
 \hline
 685 \\
 2 \\
 \hline
 4700
 \end{array}
 \qquad
 \begin{array}{r}
 4800 \quad 100 \quad 20 \quad 5 \text{ Ans} \\
 4 \overline{) 6720} \quad 140 \quad 28 \quad 7
 \end{array}$$

Reduce $70 \text{ } 4 \text{ part}$ to the fraction of A lb Troy

$$\begin{array}{r}
 12 \\
 20 \\
 \hline
 240 \\
 24 \\
 \hline
 960 \\
 480 \\
 \hline
 5760
 \end{array}
 \qquad
 \begin{array}{r}
 7 - 4 \\
 22 \quad 6 \quad 12 \\
 4 \overline{) 144} \quad 36 \quad 6 \quad 3 \text{ Answer} \\
 240 \quad 60 \quad 10 \quad 5
 \end{array}$$

Reduce $18 \text{ } 9$ to the fraction of A quire

$$2 \overline{) \frac{79}{29}} \quad \frac{9}{14} \text{ Ans}$$

Reduce $5 \text{ } 7 \frac{1}{2}$ to the fraction of A lb

$$\begin{array}{r}
 6 \\
 12 \\
 \hline
 72 \\
 4 \\
 \hline
 288
 \end{array}
 \qquad
 \begin{array}{r}
 5 - 7 - 2 \\
 12 \\
 \hline
 67 \\
 4 \\
 \hline
 272 \\
 3 \overline{) 288} \quad 90 \quad 15 \text{ Ans} \\
 288 \quad 96 \quad 16
 \end{array}$$

Continued

Reduce $21 \frac{1}{5}$ to the fraction of a
minutere

$$\begin{array}{r} 36 \\ 12 \\ \hline 72 \\ 36 \\ \hline 108 \\ 432 \\ \hline 2160 \end{array}$$

$$\begin{array}{r} 21 = 7 - \frac{1}{5} \\ \frac{12}{12} \\ 254 \\ \hline 6 \overline{) 1296} \quad 216 \quad 36 \quad 6 \quad 2 \\ \underline{2160} \quad 360 \quad 60 \quad 10 \quad 5 \end{array} \quad \text{Ans}$$

Addition of Vulgar Fractions

Examples

Add $7 \frac{4}{5}$ $\frac{5}{5}$ of $\frac{3}{8}$ and 7 together

$$\begin{array}{r} 7 \frac{4}{5} \\ \frac{5}{5} \\ \hline 79 \\ 5 \end{array} \quad \begin{array}{r} 5 \frac{3}{8} \\ \frac{5}{5} \\ \hline 56 \\ 15 \end{array} \quad \begin{array}{r} 7 \\ \frac{15}{56} \end{array}$$

$$\begin{array}{r} 79 \\ 56 \\ \hline 280 \end{array} \quad \begin{array}{r} 39 \quad 15 \quad 7 \\ \hline 5 \quad 56 \quad 1 \\ \hline 15 \quad 39 \quad 56 \\ \hline 75 \quad 304 \quad 168 \\ \hline 2184 \end{array} \quad \begin{array}{r} 7 \\ \hline 56 \\ 7 \\ \hline 39 \frac{7}{5} \\ \hline 1980 \\ 2184 \\ \hline 75 \end{array}$$

$$\begin{array}{r} 280 \overline{) 4219} \quad 15 \frac{79}{280} \quad \text{Ans} \\ \underline{280} \\ 1419 \\ \underline{1400} \\ 19 \end{array}$$

Continued

What is the sum of $\frac{7}{10}$ of $4\frac{5}{8}$ $\frac{3}{4}$ of $\frac{1}{3}$ and $\frac{9}{4}$

$$\begin{array}{r} 7 \quad 2 \quad 4 \quad 5 \\ 10 \quad 8 \quad 8 \quad 8 \\ \hline 37 \\ 8 \end{array}$$

$$\begin{array}{r} 3 \quad 3 \quad 1 \\ 12 \quad 4 \end{array}$$

$$\begin{array}{r} 9 \quad 1 \\ 4 \quad 4 \\ \hline 37 \\ 4 \end{array}$$

$$\begin{array}{r} 7 \quad 37 \quad 1 \quad 37 \\ 10 \quad 8 \quad 4 \quad 4 \\ \hline 37 \\ 40 \\ 70 \\ 370 \\ 70 \\ 370 \\ 259 \end{array}$$

$$\begin{array}{r} 259 \quad 1 \quad 37 \\ 259 \quad 4 \quad 4 \\ \hline 259 \\ 4 \\ 320 \quad 1036 \\ 4 \\ 4144 \end{array}$$

$$\begin{array}{r} 37 \\ 4 \\ \hline 148 \\ 40 \\ 11840 \\ 4144 \\ 320 \end{array}$$

$$\begin{array}{r} 40 \\ 4 \\ \hline 320 \\ 1280 \end{array}$$

$$\begin{array}{r} 1280 \overline{) 16304} \quad 12 \quad 244 \text{ Ans} \\ \underline{1280} \\ 3504 \\ \underline{2560} \\ 944 \end{array}$$

Continued

57

Add $\frac{3}{4}$ and $\frac{4}{5}$ of penny together

$$\begin{array}{r} 20 \quad 12 \\ 3 \quad 1 \quad 1 \\ \hline \end{array}$$

$$\begin{array}{r} 20 \quad 12 \\ 3 \overline{) 240} \quad 80 \\ \underline{9} \quad 3 \end{array}$$

$$\begin{array}{r} 3 \quad 12 \quad 12 \\ 7 \quad 1 \quad 36 \\ \hline 7 \end{array}$$

$$\begin{array}{r} 80 \quad 36 \quad 4 \\ 3 \quad 7 \quad 5 \\ \hline 36 \quad 80 \\ 108 \quad 560 \\ \hline 540 \quad 2800 \end{array}$$

$$\begin{array}{r} 74 \\ 28 \\ 3 \\ \hline 84 \end{array}$$

$$\begin{array}{r} 2800 \\ 540 \\ \hline \end{array}$$

$$\begin{array}{r} 5 \\ 7 \\ 35 \\ 3 \\ \hline 105 \end{array}$$

$$105 \overline{) 3424} \quad (32 \text{ p 1 Answer}$$

$$\begin{array}{r} 315 \\ 274 \\ 210 \\ 64 \end{array} \quad 14 \overline{) 3212} - 8 \frac{64}{105} \text{ Answer}$$

Add $\frac{1}{4}$ of week $\frac{1}{3}$ of day $\frac{1}{2}$ of an hour and $\frac{1}{4}$ of a minute together

$$\begin{array}{r} 1 \quad 7 \quad 24 \quad 60 \\ 4 \quad 1 \quad 1 \quad 1 \\ \hline \end{array}$$

$$\begin{array}{r} 24 \quad 60 \\ 3 \quad 1 \quad 1 \\ \hline \end{array}$$

$$\begin{array}{r} 1 \quad 60 \\ 2 \quad 1 \\ \hline \end{array}$$

$$4 \overline{) 10080} \quad (2520$$

$$\begin{array}{r} 60 \\ 24 \\ 240 \\ 120 \\ \hline 480 \end{array}$$

$$\begin{array}{r} 2 \overline{) 60} \quad 30 \\ 2 \quad 1 \\ \hline \end{array}$$

$$\begin{array}{r} 2520 \quad 480 \quad 30 \quad 3 \\ 1 \quad 1 \quad 1 \quad 4 \\ \hline 480 \quad 2520 \quad 3 \quad 30 \\ 4 \quad 3 \quad 120 \\ \hline 1920 \quad 10080 \end{array}$$

$$\begin{array}{r} 10080 \\ 120 \\ 3 \end{array}$$

$$40 \overline{) 3030} \quad (50 \frac{2}{2}$$

$$4 \overline{) 12123}$$

$$3030 - 3$$

$$4 \overline{) 180} \quad 45$$

Answer day 2 hours 3 minutes 45 seconds

54 Subtraction of vulgar Fractions

Examples

From $\frac{3}{4}$ take $\frac{2}{5}$ of $\frac{5}{8}$

$$\begin{array}{r} \frac{3}{4} \\ \frac{1}{5} \\ \hline \frac{2}{20} \end{array} \quad \begin{array}{r} \frac{5}{8} \\ \frac{2}{5} \\ \hline \frac{10}{40} \end{array} \quad \begin{array}{r} \frac{2}{5} \\ \frac{10}{40} \\ \hline \frac{28}{40} \end{array}$$

Answer $\frac{18}{40}$

From $\frac{49}{50}$ take $\frac{5}{10}$

$$\begin{array}{r} \frac{49}{50} \\ \frac{5}{10} \\ \hline \frac{44}{50} \end{array}$$

Answer $\frac{44}{50}$

From $\frac{149}{4}$ take $\frac{137}{7}$

$$\begin{array}{r} \frac{149}{4} \\ \frac{137}{7} \\ \hline \frac{1043}{28} \end{array}$$

Answer $\frac{1043}{28}$

From $\frac{1}{4}$ of $\frac{1}{2}$ take $\frac{1}{10}$ of $\frac{1}{2}$ shilling

$$\begin{array}{r} \frac{1}{4} \\ \frac{1}{2} \\ \hline \frac{1}{8} \end{array} \quad \begin{array}{r} \frac{1}{2} \\ \frac{1}{10} \\ \hline \frac{1}{10} \end{array}$$

Answer $\frac{1}{10}$

Continued

59

D

From $\frac{5}{4}$ of an ounce take $\frac{3}{4}$ of a part

$$\frac{5}{7} \quad \frac{20}{1}$$

$$\frac{20}{100}$$

$$\frac{3}{4}$$

$$\frac{7}{4} \quad \frac{28}{28}$$

$$\frac{7}{3} \quad \frac{21}{21}$$

$$\frac{100}{400}$$

$$\frac{21}{421}$$

28/379 (13 Ans 13 part
12 grains

$$\frac{28}{28}$$

$$\frac{28}{28}$$

$$\frac{28}{28}$$

$$\frac{28}{28}$$

$$\frac{28}{28}$$

$$\frac{28}{28}$$

$$\frac{28}{28}$$

$$\frac{28}{28}$$

$$\frac{28}{28}$$

$$\frac{28}{28}$$

$$\frac{28}{28}$$

$$\frac{28}{28}$$

$$\frac{6}{7}$$

Multiplication of Vulgar Fractions

Examples

What is the continued product of $\frac{1}{3}$, $\frac{1}{5}$, $\frac{1}{7}$, $\frac{1}{8}$ and 6

$$\begin{array}{r} 4111976 \\ 335481 \\ \hline 13 \\ 3 \end{array}$$

$$\begin{array}{r} 93176 \\ 35321 \\ \hline 15 \\ 32 \\ 30 \\ 450 \\ 480 \end{array}$$

480/480 (1 11/80 Ans 2

Continued

Multiply $\frac{4}{17}$ by $\frac{5}{2}$ ✓

$$\begin{array}{r} \frac{4}{17} \times \frac{5}{2} = \frac{20}{34} = \frac{10}{17} \end{array}$$

Answer ✓

Multiply $\frac{3}{5}$ by $\frac{2}{3}$ ✓

$$\frac{3}{5} \times \frac{2}{3} = \frac{6}{15} = \frac{2}{5}$$

$$\frac{5}{3} \times \frac{6}{2} = \frac{30}{6} = 5$$

Answer ✓

Division of Vulgar Fractions
Examples ✓

Divide $\frac{1}{3}$ by $\frac{2}{3}$ ✓

$$\frac{1}{3} \div \frac{2}{3} = \frac{1}{3} \times \frac{3}{2} = \frac{1}{2}$$

$$\frac{17}{3} \div \frac{2}{7} = \frac{17}{3} \times \frac{7}{2} = \frac{119}{6} = 19 \frac{5}{6}$$

Ans ✓

$$\begin{array}{r} 5 \\ 21 \overline{) 105} \\ \underline{105} \\ 0 \end{array}$$

50	17
----	----

$$\begin{array}{r} 17 \\ 5 \\ \hline 22 \end{array}$$

$$\begin{array}{r} 183 \\ 145 \\ \hline 38 \end{array}$$

$$\begin{array}{r} 11 \\ 8 \\ \hline 19 \end{array} \quad \begin{array}{r} 4 \\ 3 \\ 8 \\ \hline 248 \end{array} \quad \begin{array}{r} 11 \\ 4 \\ \hline 154 \end{array}$$

4/764 41 - Answer
248 62

$$\begin{array}{r} 9 8 \\ \hline 1 3 \end{array}$$

$$\begin{array}{r} 88 \\ 3 \overline{) 304} \\ \underline{24} \\ 64 \\ \underline{60} \\ 4 \end{array}$$

$$\begin{array}{r} 77112 \\ 4 \overline{) 34848} \\ \underline{28} \\ 68 \\ \underline{64} \\ 48 \\ \underline{44} \\ 48 \\ \underline{44} \\ 48 \\ \underline{44} \\ 48 \end{array}$$

~~$$\begin{array}{r}
 6 \\
 25225 \\
 \hline
 201800
 \end{array}$$~~

$$\begin{array}{r} 25225 \quad 8 \\ \hline 6 \quad 784 \\ 6 \end{array}$$

$$\begin{array}{r} 25225 \\ 1704 \overline{) 201800} \\ \underline{18816} \\ 136640 \\ \underline{136640} \\ 0 \end{array}$$

$$\begin{array}{r} 13640 \\ 4408 \\ \hline 4232 \quad 524 \\ 4504 \quad 588 \end{array}$$

Addition of Decimal Fractions

Examples

Find the sum of 19.073 + 2.3597 + 223 + 50197581

+ 3498.1 + 12.358

19.073	
2.3597	
223	
50197581	
3498.1	
12.358	

3734 9104 581 the sum required

Required the sum of 429 + 21.57 + 355.073 + 1.07

+ 17

429	
21.57	
355.073	
1.07	
17	
808	2143

the sum required

Subtraction of Decimal Fractions

Examples

From 171.195 take 125.9176

171.195
125.9176

45.2774 Answer

From 219.9384 take 195.91

219.9384
195.91

23 = 2284 Answer

Multiplication of Decimals

Examples

Multiply .02345 by .00163

$$\begin{array}{r}
 .02345 \\
 \times .00163 \\
 \hline
 07035 \\
 14090 \\
 \hline
 .0000382235 \text{ Answer}
 \end{array}$$

Multiply 25.238 by 12.17

$$\begin{array}{r}
 25.238 \\
 \times 12.17 \\
 \hline
 176.666 \\
 252.238 \\
 504.776 \\
 25238 \\
 \hline
 307.145646 \text{ Answer}
 \end{array}$$

It is required to multiply 56.7534916 by 5.376728 and to retain only five decimal places in the product.

$$\begin{array}{r}
 56.7534916 \\
 \times 5.376728 \\
 \hline
 4540279328 \\
 1135069832 \\
 5107814244 \\
 3405209496 \\
 2702744412 \\
 1702604748 \\
 273767480 \\
 \hline
 305.15943428
 \end{array}$$

Division of Decimal Fractions Examples

$$\begin{array}{r}
 219 \overline{) 219841075} \quad (1000538087 \\
 \underline{1095} \\
 834 \\
 \underline{657} \\
 1771 \\
 \underline{1752} \\
 1909 \\
 \underline{1752} \\
 1555 \\
 \underline{1536} \\
 22
 \end{array}$$

$$\begin{array}{r}
 3719 \overline{) 380000} \quad (102178 \\
 \underline{3719} \\
 8100 \\
 \underline{7438} \\
 6620 \\
 \underline{3719} \\
 29010 \\
 \underline{26033} \\
 29770 \\
 \underline{29952} \\
 18
 \end{array}$$

$$\begin{array}{r}
 133 \overline{) 5939} \quad (43135.3 \\
 \underline{532} \\
 417 \\
 \underline{399} \\
 180 \\
 \underline{133} \\
 470 \\
 \underline{399} \\
 710 \\
 \underline{665} \\
 450 \\
 \underline{399} \\
 51
 \end{array}$$

$$\begin{array}{r}
 72 \overline{) 918.217} \quad (12.753 \text{ Answer} \\
 \underline{72} \\
 198 \\
 \underline{144} \\
 542 \\
 \underline{504} \\
 381 \\
 \underline{360} \\
 217 \\
 \underline{216} \\
 1
 \end{array}$$

$$\begin{array}{r}
 3709 \overline{) 20059376} \quad (20156 \\
 \underline{3709} \\
 2147 \\
 \underline{1895} \\
 2524 \\
 \underline{2274} \\
 250
 \end{array}$$

Continued

165

$$99.5678 \overline{) 4.6789837548} \text{ (0469931 quotient)}$$

$$3 \ 982712$$

$$99.567 \overline{) 4.96271}$$

$$5 \ 97402$$

$$99.56 \overline{) 4.98869}$$

$$8 \ 9604$$

$$99 \overline{) 310}$$

$$2 \ 97$$

$$9 \overline{) 13}$$

$$9$$

$$4$$

Remainder

Reduction of Decimals

Examples

Reduce $\frac{1}{2}$ to a decimal

$$4/10 \text{ or } .25 \text{ Answer}$$

Reduce $\frac{3}{4}$, $\frac{5}{8}$ and $\frac{7}{16}$ to decimals

$$\frac{3}{4} = .75 \quad \frac{5}{8} = .625 \quad \frac{7}{16} = .4375$$

Reduce $\frac{1}{4}$, $\frac{1}{2}$, $\frac{3}{4}$, $\frac{1}{3}$, $\frac{4}{5}$, $\frac{5}{6}$ and $\frac{7}{8}$ to decimals

$$\frac{1}{4} = .25 \quad \frac{1}{2} = .50 \quad \frac{3}{4} = .75 \quad \frac{1}{3} = .333 \quad \frac{4}{5} = .80 \quad \frac{5}{6} = .833 \quad \frac{7}{8} = .875$$

$$4/10 \text{ (.25)} \quad 2/10 \text{ (.2)} \quad 4/10 \text{ (.4)} \quad 3/10 \text{ (.3)} \quad 5/40 \text{ (.125)} \quad 6/50 \text{ (.12)} \quad 7/50 \text{ (.14)}$$

$$4/10 \text{ (.4)} \quad 6/10 \text{ (.6)} \quad 8/10 \text{ (.8)} \quad 9/10 \text{ (.9)}$$

Answers: .25, .5, .75, .333, .8, .833, .875

Case 2nd

Examples

Reduce $17\ 5\ \frac{3}{4}$ to the Decimal of A pound

4	3.
12	4. 75
20	17. 729166, &c
	1884458

Reduce 1. 2. 3. 4 and so on to 19 pence to Decimals

$$20/1.00/.5 \quad 20/2.00/.7 \quad 20/3.00/.15 \quad 20/4.00/.2 \quad 20/5.00/.25$$

$$20/6.00/.3 \quad 20/7.00/.35 \quad 20/8.00/.4 \quad 20/9.00/.45 \quad 20/10.00/.5$$

$$20/11.00/.55 \quad 20/12.00/.6 \quad 20/13.00/.65 \quad 20/14.00/.7$$

$$20/15.00/.75 \quad 20/16.00/.8 \quad 20/17.00/.85 \quad 20/18.00/.9$$

$$20/19.00/.95 \quad \text{Answer}$$

Reduce 1234 &c to 11 Pence to the Decimal of A £

$$12/1.00/.83 \quad 12/2.00/.866 \quad 12/3.00/.925 \quad 12/4.00/.933$$

$$12/5.00/.9416 \quad 12/6.00/.95 \quad 12/7.00/.9583 \quad 12/8.00/.9666$$

$$12/9.00/.975 \quad 12/10.00/.9833 \quad 12/11.00/.9916 \quad \text{Answer}$$

Reduce $13\ 5\ \frac{1}{2}$ to the Decimal of A £

4	2
12	5. 5
20	13. 458
	6929 Answer

Continued

Reduce 23 13 part 9 grains to the decimal of a Troy

24	9
20	13.375
12	10.66875
	44.2025 Ans

Case Bnd

Examples

Find the decimal of 13 lb 9 $\frac{3}{4}$ by inspection

$$2/13 \text{ (6 1/2)} \quad \frac{9 \frac{3}{4}}{\frac{4}{4}} = \frac{39}{4}$$

$$\begin{array}{r} 18.5 \\ 39 \\ 2 \\ \hline 24 \end{array} \frac{2}{91} \text{ decimal required}$$

Find by inspection the decimal expression of 13 lb 9 $\frac{3}{4}$ and 17 lb 4 $\frac{1}{2}$

$$\begin{array}{r} 2/13 \quad 3 \frac{1}{2} \\ 9 \quad 15 \\ 13 \\ \hline 1 \\ 914 \text{ Answer} \end{array}$$

$$\begin{array}{r} 2/17 \quad 4 \frac{1}{2} \\ 8 \frac{1}{2} \quad 33 \\ \hline 16 \end{array}$$

$$\begin{array}{r} 5 \\ 33 \\ 2 \\ \hline 485 \text{ Answer} \end{array}$$

Case 4th

Examples

Find the value of 9396²⁰/₁₂ of a pound

14/9396²⁰/₁₂

9/52320

12/09280

Ans 14 Shilling 9¹⁰/₁₂

What is the value of 679 of a shilling

679

12

1358

679

8148

Ans 8¹⁴/₁₂ 8

What is the value of 5446²⁾/₅ of a degree

5446²⁾/₅

76221

50814

4234 - 1

5446²⁾/₅

5446²⁾/₅

5446²⁾/₅

4768760

40

35/0400

5¹/₂

2000

0200

2200

3

6600

12

9/200

3

2/7600

Answer 54 Miles

56 Furlongs

35 Rods 7 inches

2 Barlecorns 7600

Case 5th

69

Examples

Find the value of 976 by inspection

$$\begin{array}{r} 4 \text{ shillings} \\ 2 \\ 14 \\ 1 \end{array} \quad \begin{array}{r} 76 \\ 4 \overline{) 26} \\ 6 - 2 \\ 6 - 1 \end{array} \quad \begin{array}{l} \text{farthings} \\ 17 = \frac{1}{4} \text{ Answer} \end{array}$$

Value the following decimals by inspection and find their sums viz £745 ... £537 ... £916 ... £74 ... £5 ... £25 ... £09 £008

$$\begin{array}{r} 745 \\ 5 \overline{) 35} \\ 14 \overline{) 14} \\ 1 \overline{) 1} \\ 15 \end{array} \quad \begin{array}{r} 537 \\ 5 \overline{) 35} \\ 10 \end{array} \quad \begin{array}{r} 916 \\ 9 \overline{) 15} \\ 3 \frac{3}{4} \end{array} \quad \begin{array}{r} 74 \\ 2 \overline{) 14} \\ 4 \overline{) 34} \\ 9 = 2 \end{array}$$

$$\begin{array}{r} 9 \\ 2 \\ 18 \end{array}$$

$$\begin{array}{r} 5 \\ 2 \\ 10 \end{array}$$

$$\begin{array}{r} 25 \\ 2 \overline{) 5} \\ 12 \\ 1 \\ 5 \end{array}$$

$$\begin{array}{r} 9 \\ 2 \\ 18 \\ 09 \end{array}$$

$$\begin{array}{r} 09 \\ 5 \\ 45 \\ 4 \overline{) 18} \\ 9 = 2 \end{array}$$

$$\begin{array}{r} 008 \\ 4 \overline{) 8} \\ 2 \end{array}$$

15	—	4	—	2
10	—	4	—	3
94	—	3	—	3
14	—	9	—	2
10	—	0	—	0
05	—	0	—	0
01	—	9	—	2
00	—	2	—	0

$$\begin{array}{r} 15 \\ 10 \\ 94 \\ 14 \\ 10 \\ 05 \\ 01 \\ 00 \end{array} \quad \begin{array}{r} 16 \\ 6 \\ 0 \end{array} \quad \begin{array}{r} 16 \\ 6 \\ 0 \end{array}$$

Answer

100 Rule of Three in Vulgar Fractions

Examples

If $\frac{5}{8}$ of a yard cost $\frac{5}{10}$ of a pound what will $\frac{9}{15}$ of Ell English cost

$$\begin{array}{r} \frac{5}{8} \quad \frac{4}{1} \quad \frac{1}{5} \\ \hline \frac{5}{8} \quad \frac{4}{1} \quad \frac{1}{5} \\ \hline 40 \end{array}$$

$$\begin{array}{r} \frac{2}{1} \quad \frac{5}{7} \quad \frac{9}{15} \\ \hline \frac{2}{1} \quad \frac{5}{7} \quad \frac{9}{15} \\ \hline 105 \end{array}$$

If $\frac{3}{5}$ of a yard cost $\frac{1}{2}$ what will $\frac{4}{5}$ of a yard cost

$$\begin{array}{r} \frac{3}{5} \quad \frac{4}{5} \quad \frac{1}{2} \\ \hline \frac{3}{5} \quad \frac{4}{5} \quad \frac{1}{2} \\ \hline 48 \end{array}$$

$$\begin{array}{r} \frac{1}{2} \quad \frac{9}{10} \\ \hline \frac{1}{2} \quad \frac{9}{10} \\ \hline 105 \end{array}$$

$$\begin{array}{r} \frac{4}{5} \quad \frac{1}{2} \quad \frac{1}{2} \\ \hline \frac{4}{5} \quad \frac{1}{2} \quad \frac{1}{2} \\ \hline 105 \end{array}$$

$$\begin{array}{r} \frac{1}{2} \quad \frac{9}{10} \\ \hline \frac{1}{2} \quad \frac{9}{10} \\ \hline 105 \end{array}$$

$$\begin{array}{r} \frac{4}{5} \quad \frac{1}{2} \quad \frac{1}{2} \\ \hline \frac{4}{5} \quad \frac{1}{2} \quad \frac{1}{2} \\ \hline 105 \end{array}$$

If 70 Bushels of corn cost $12\frac{3}{4}$ what is it per Bushel

$$\begin{array}{r} 12\frac{3}{4} \\ \hline 12\frac{3}{4} \\ \hline 5 \end{array}$$

$$\begin{array}{r} \frac{1}{2} \quad \frac{5}{10} \quad \frac{1}{1} \\ \hline \frac{1}{2} \quad \frac{5}{10} \quad \frac{1}{1} \\ \hline 350 \end{array}$$

If $\frac{7}{16}$ of a ship cost $\frac{1}{2}$ what are $\frac{3}{2}$ of her worth

$$\begin{array}{r} \frac{7}{16} \quad \frac{1}{2} \quad \frac{3}{2} \\ \hline \frac{7}{16} \quad \frac{1}{2} \quad \frac{3}{2} \\ \hline 224 \end{array}$$

$$\begin{array}{r} \frac{1}{2} \quad \frac{5}{10} \quad \frac{1}{1} \\ \hline \frac{1}{2} \quad \frac{5}{10} \quad \frac{1}{1} \\ \hline 350 \end{array}$$

$$\begin{array}{r} \frac{1}{2} \quad \frac{5}{10} \quad \frac{1}{1} \\ \hline \frac{1}{2} \quad \frac{5}{10} \quad \frac{1}{1} \\ \hline 350 \end{array}$$

Continued

At $3\frac{5}{8}$ per unit what will $9\frac{2}{3}$ lb come to

$$\begin{array}{r} 3\frac{5}{8} \\ \times 8 \\ \hline 29 \end{array}$$

$$\begin{array}{r} 9\frac{2}{3} \\ \times 3 \\ \hline 29 \end{array}$$

$$\begin{array}{r} 1 = 29 = 29 \\ \hline 112 = 8 = 3 \end{array}$$

$$\begin{array}{r} 29 \\ \hline 29 \end{array}$$

$$\begin{array}{r} 896 \\ \times 3 \\ \hline 2688 \end{array}$$

$$\begin{array}{r} 261 \\ \times 1 \\ \hline 261 \end{array}$$

Answer $26\frac{1}{2}$ 56

$$\begin{array}{r} 2688 \overline{) 16820} (6 \\ \underline{16128} \end{array}$$

$$\begin{array}{r} 692 \\ \times 2 \\ \hline 1384 \end{array}$$

$$\begin{array}{r} 2688 \overline{) 5304} (2 \\ \underline{5376} \end{array}$$

A person having $\frac{1}{5}$ of a vessel sells $\frac{2}{3}$ of his share for £319

$$\begin{array}{r} 8 \overline{) 240} (30 \\ \underline{240} \end{array} \quad \begin{array}{r} 6 \overline{) 30} (5 \\ \underline{30} \end{array}$$

what is the whole vessel worth?

$$\begin{array}{r} 4 \overline{) 2} (\frac{1}{2} \\ \underline{4} \\ 5 \overline{) 3} (\frac{3}{5} \\ \underline{15} \end{array} \quad \begin{array}{r} 15 \\ \times 1 \\ \hline 15 \end{array} \quad \begin{array}{r} 319 \\ \times 1 \\ \hline 319 \end{array}$$

$$\begin{array}{r} 8 \overline{) 319} (39 \\ \underline{240} \end{array}$$

Answer £39 56

$$\begin{array}{r} 225 \\ \times 2 \\ \hline 450 \end{array} \quad \begin{array}{r} 20 \\ \times 2 \\ \hline 40 \end{array} \quad \begin{array}{r} 48 \\ \times 6 \\ \hline 288 \end{array}$$

Continued

A merchant sold $3\frac{1}{2}$ pieces of cloth each containing $12\frac{2}{3}$ yards at $9\frac{1}{2}$ shillings per yard what did the whole Amount to

$\begin{array}{r} 51 \\ \underline{22} \\ 11 \\ \underline{2} \\ 3 \\ \underline{6} \end{array}$	$\begin{array}{r} 122 \\ \underline{33} \\ 38 \\ \underline{3} \\ 38 \\ \underline{38} \\ 209 \end{array}$	$\begin{array}{r} 9-12 \\ \underline{11} \\ 108 \\ \underline{2} \\ 217 \end{array}$
--	--	--

$\begin{array}{r} 1 \\ \underline{1} \\ 2 \\ \underline{3} \\ 6 \end{array}$	$\begin{array}{r} 217 \\ \underline{2} \\ 3 \\ \underline{6} \end{array}$	$\begin{array}{r} 209 \\ \underline{217} \\ 1163 \end{array}$	$\begin{array}{r} 209 \\ \underline{217} \\ 1163 \end{array}$	$\begin{array}{r} 12 \\ 20 \\ 629(317 \\ \underline{65} \\ 29 \\ \underline{20} \\ 99 \end{array}$
--	---	---	---	--

Ans 317 90 10 $\frac{3}{5}$

A merchant makes insurance upon A vessel and cargo valued at £ 3750 16 S at 15% quinees per cent what does the premiums Amount to

$\begin{array}{r} 100 \\ \underline{20} \\ 2000 \\ \underline{20} \\ 20 \end{array}$	$\begin{array}{r} 3750-16 \\ \underline{20} \\ 75016 \\ \underline{20} \\ 20 \end{array}$	$\begin{array}{r} 15-14 \\ \underline{28} \\ 124 \\ \underline{31} \\ 434 \\ \underline{20} \end{array}$
--	---	--

Ans 434 20

Continued

$$\begin{array}{r} 800000 \overline{) 651138880} \quad (813 \\ 6400000 \\ \hline 1113888 \\ 800000 \\ \hline 3138880 \\ 2400000 \\ \hline 738880 \\ 20 \end{array}$$

Rule of Three in

Example 8

$$\begin{array}{r} 800000 \overline{) 14777600} \quad (18 \\ 800000 \\ \hline 6777600 \\ 6400000 \\ \hline 377600 \\ 12 \end{array}$$

$$\begin{array}{r} 800000 \overline{) 4531200} \quad (5 \\ 400000 \\ \hline 5312 \\ 4 \end{array}$$

$$\begin{array}{r} 8000 \overline{) 21248} \quad (2 \\ 16000 \\ \hline 5248 \end{array}$$

Ans 813 \pm 18 5 $\frac{2}{12}$

If one ounce of silver
be 14^d what is the
price of a bowl that
weighs 1^{lb} 7^{oz} 13^{gr}
1 = 5 = 8 = 1 = 7 = 13

$$\begin{array}{r} 20 \\ 20 \\ \hline 40 \\ 40 \end{array} \quad \begin{array}{r} 12 \\ 12 \\ \hline 24 \\ 24 \end{array} \quad \begin{array}{r} 12 \\ 12 \\ \hline 24 \\ 24 \end{array}$$

$$\begin{array}{r} 390 \\ 24 \\ \hline 1593 \\ 1593 \\ \hline 9433 \end{array}$$

$$\begin{array}{r} 48 \overline{) 17308} \quad 48 \overline{) 1824} \\ 48 \\ \hline 250 \\ 240 \\ \hline 106 \\ 96 \\ \hline 104 \\ 96 \\ \hline 8 \end{array} \quad \begin{array}{r} 40 \overline{) 126} = 10 \\ 40 \\ \hline 6 \end{array}$$

Answer 6 £ 6 5 10^d 1^s

Sum 7th 1809

Duodecimals

Examples

Multiply 9 ft 8' 6" by 7 ft 9' 3"

$$\begin{array}{r}
 9 = 8 = 6 \\
 7 = 9 = 3 \\
 \hline
 67 = 11 = 6 \\
 7 = 3 = 4 = 6 \\
 \hline
 2 = 5 = 1 = 6 \\
 \hline
 75 = 5 = 9 = 7 = 6
 \end{array}$$

How many square feet in a board 17 feet 7 inches long & 1 foot 5 inches wide

$$\begin{array}{r}
 17 = 13 \\
 1 = 5 \\
 \hline
 13 = 9 \\
 9 = 3 = 11 \\
 \hline
 24 = 10 = 11
 \end{array}$$

Ans 24 = 10 = 11

Suppose a board of wood to measure 8 ft long 4 ft wide 4 ft high how many square feet

$$\begin{array}{r}
 8 \\
 4 \\
 \hline
 32 \\
 4 \\
 \hline
 16/128 \text{ feet}
 \end{array}$$

Suppose a board of wood to measure 8 feet

long 3 1/2 feet long wide 2 1/2 high

$$\begin{array}{r}
 8 = 0 \\
 3 = 6 \\
 \hline
 24 = 0 \\
 4 = 0 = 0 \\
 \hline
 28 = 0 = 0 \\
 2 = 4 \\
 \hline
 36 = 0 = 0 \\
 14 = 0 = 0 = 0 \\
 \hline
 70 = 0 = 0 = 0
 \end{array}$$

$$\begin{array}{r}
 16/70 \text{ (4)} \\
 64 \\
 \hline
 276 \text{ } 3 \\
 16 \text{ } 8
 \end{array}$$

Answer 4 feet 3/8

Continued

Suppose I had a board to measure
 4 1/2 feet in length 4 feet wide 5 1/2 high
 how many square feet and what

4 = 6 would it cost at 1/4 = 25 per board

$$\begin{array}{r} 34 = 0 \\ 5 = 6 \\ 170 = 0 \\ 17 = 0 = 0 \\ \hline 187 = 0 = 0 \end{array}$$

128 - 125 = 3

$$\begin{array}{r} 128723375 \\ - 125 \\ \hline 935 \\ 374 \\ 187 \\ \hline 128723375 \end{array}$$

$$\begin{array}{r} 128723375 \\ - 256 \\ \hline 128723119 \end{array}$$

Answered 1 = 82 = 6

Practice

Examples

What is the value of 468 yards at 2/9 1/4

Per yard

$$\begin{array}{r} 2-6 \\ 3- \\ \hline 1/4 \cdot 468 = 117 \\ 1/4 \cdot 117 = 29.25 \\ \hline 146.25 = 146 = 7 \end{array}$$

$$\begin{array}{r} 4/11553 \text{ yds at } 1/4 \text{ per yard} \\ 12/438 = 1 \\ 20/36 = 5 \\ \hline 1 = 16 \end{array}$$

Answered 1 = 16 = 6 1/4

(continued)

2 1753 at $\frac{1}{2}$ per yd
12 876-1

20 713-2
 $\underline{13-13=0}$

16 1753 at $\frac{3}{4}$ per yd
20 109-6-3
 $\underline{15-9=6=3}$ Ans

12 1753 at 10 per yd
 $\underline{146=1}$
 $\underline{17=5-1}$ Ans

4 1753 at $1\frac{1}{4}$ per yd
 $\underline{487=1}$
12 21. 91-17
20 18(2=7)
 $\underline{29=2-7=1}$ Ans

Case 2nd

Examples

What 487 $\frac{1}{2}$ yds
come to at 5 per yd

$\frac{1}{2}$ 487-6
 $\frac{1}{12}$ 162=8
20 40-7=2
 $\underline{203=1=2}$
 $\underline{17=3=1=2}$ Ans

Case 3rd

Examples

What is the value
of 3795 $\frac{1}{4}$ at
 $\frac{1}{4}$ per yd

4 3795
12 943-1
20 719-
 $\underline{13-19=0\frac{3}{4}}$ Answer

Case 4th

Examples

What is the value
of 59 $\frac{1}{4}$ yards
at 15 20 per yd

2 591-3
 $\underline{98-6=2}$
40 6819=9-2
 $\underline{434=9=9\frac{1}{2}}$

Answer 134
729 $29\frac{1}{2}$

Simple Interest

Examples

Required the Interest of 700 Dollars for 4 years at 6 per cent per year

$$\begin{array}{r} \$ 700 \\ \times 4 \\ \hline 2800 \\ \times 6 \\ \hline 16800 \end{array}$$

Required the Interest of \$735 for 5 years 4 months at 5 per cent

$$\begin{array}{r} \$ 735 \\ \times 5 \\ \hline 3675 \\ \times 5\frac{1}{3} \\ \hline 18375 \\ 1225 \\ \hline 19600 \end{array}$$

\$196 Answer

Required the Interest of 3520 Dollars for 2 1/2 years at 5 1/4 per cent.

$$\begin{array}{r} \$ 3520 \\ \times 2\frac{1}{2} \\ \hline 17600 \\ \times 2\frac{1}{4} \\ \hline 8800 \\ \hline 218400 \\ \times 2\frac{1}{2} \\ \hline 36960 \\ 924 \\ \hline 46200 \end{array}$$

\$462 = 00 Answer

Continued

Required the Interest of \$720 for 10 weeks
at 5 1/2 per cent

$$\begin{array}{r} \$720 \\ \times 5\frac{1}{2} \\ \hline 3600 \\ 36 \\ \hline 3960 \end{array}$$

Weeks 52 - 39 = 13 = 10

$$52 \overline{) 39600} \begin{array}{l} 767 \\ 364 \\ \hline 320 \\ 312 \\ \hline 80 \\ 52 \\ \hline 28 \end{array}$$

Answer \$7 = 61 = 5

$$52 \overline{) 2800} \begin{array}{l} 53 \\ 260 \\ \hline 20 \end{array}$$

Of \$74 Dollars 74 cents from
Jan. 4th 1795 to May 19th 1796
at 6 per cent per year

Days Mon Days
1795 = 4 = 19
1796 = 0 = 4

\$74 = 74

1 = 4 = 15 12 = 3 | 4088 = 44 One year
1348 - 44 Int 4 months
2) 339 = 33 Int one month
168 = 68 1/2 months

Int \$74 = 74 half the months
8 1/4

$$\begin{array}{r} 3397 = 92 \\ 168 = 68 \\ \hline 5566 = 60 \end{array}$$

55 66 = 60 \$55 = 66 = 6

\$55 = 66 = 6 Answer

Required the Interest of \$49 1/2 Dollars
from April 4th 1794 to November
24th 1795 at 6 per cent

1796 = 10 = 24
1793 = 3 = 4
3 7 = 20

\$49 1/2 = 50 1/2

$$349 = 50$$

$$6990 = 0$$

$$94 \overline{) 899} = 00$$

$$293 =$$

Continued

What is the Interest of $49\frac{1}{4}$ Dollars from
March 16th 1792 to October 25th 1792
at 7 per cent per year

$$\begin{array}{r} \$49 = 25 \\ \quad 7 \\ \hline 2 \overline{) 344} = 75 \\ \quad 5 \\ \hline 2068 = 50 \\ \quad 172 = 37 \\ \quad 28 = 72 \\ \quad 5 = 74 \\ \quad 2 = 87 \\ \hline 2278 = 20 \end{array}$$

$$\begin{array}{r} 1797 = 7 = 25 \\ 1791 = 2 = 16 \\ \hline 6 = 7 = 9 \end{array}$$

Answer $\$22 \div 78 = 2$

Required the Interest of 50 Dollars from Dec. 22nd 1803 to Nov. 12th 1805 at 6 per cent

$$\begin{array}{r} 1804 = 10 - 12 \\ 1802 = 11 - 22 \\ \hline 1 = 10 = 20 \end{array}$$

$$\begin{array}{r} 3/50 \\ 11\frac{2}{3} \\ \hline 50 \\ 50 \\ \hline 16 \\ 5/66 \end{array}$$

Answer $\$5 = 66$

Required the Interest of 1000 Dollars for
5 days at 6 per cent

$$\begin{array}{r} 2/1000 \\ 6 \overline{) 500} \end{array}$$

83 onto Answer

Required the Interest of $\$150 = 25$ for 25 days
at 6 per cent

$$\begin{array}{r} \$2/150 = 25 \\ \quad 75 = 12 \\ \quad 5/6 \\ \hline 6/375 = 60 \\ (82 = 60 \end{array}$$

$\frac{5}{30} = \frac{1}{6}$ is the fraction of 25 days

Required the Interest of 20 Dollars

for 15 days

$$\begin{array}{r} 2/20 \\ 4/10 \end{array}$$

$$15/30 = \frac{1}{2}$$

$\frac{1}{2}$ is the fraction of 15 days

5 onto the Answer

Continued

Required the Interest of 50th Dollars for 10 days at 6 per cent a year

$$\begin{array}{r} 2 \overline{) 50 = 25} \\ 2 \overline{) 25 = 12 \frac{1}{2}} \\ \hline 8 = 4 \text{ cents} \end{array}$$

$\frac{1}{3}$ is the fraction of 10 days
4 cents 4 mills

Required the Interest of 350 Dollars for 20 days at 6 per cent

$$\begin{array}{r} 2 \overline{) 350} \\ \hline 175 \end{array}$$

$$\begin{array}{r} 3 \overline{) 350} \\ \hline 116 \frac{2}{3} \end{array}$$

On 350 $\frac{2}{3}$ Days 365 = 21 = 20
21/00

On 2/350
2/175
3/87-
29
115

Answer \$1.15

Ans \$1.15

$$\begin{array}{r} 365 \overline{) 420} 1 \\ \hline 365 \\ \hline 5500 \\ 365 \overline{) 5500} 15 \\ \hline 1825 \\ \hline 25 \end{array}$$

Required the Interest of 500 Dollars for 10 months 12 days at 6 per cent

$$\begin{array}{r} 2 \overline{) 500} \\ \hline 3000 \\ 2 \overline{) 1500} \\ \hline 750 \\ 3 \overline{) 750} \\ \hline 250 \\ 3 \overline{) 250} \\ \hline 83 = 33 \\ 12.66 \end{array}$$

On by half the number of months
5/500 $\frac{1}{5}$ 10 months 12 days
2500 $\frac{1}{5}$
100
26/00

5 $\frac{1}{5}$ fraction

25/99 = 99 Answer

Required the Interest of 20 Dollars 2 months at 6 per cent

120 cents
The Answer

Continued

Required the Interest of 1000 Dollars for 8 months
at 6 per cent

$$\begin{array}{r} 1000 \\ \times 4000 \\ \hline 4000 \end{array} \text{ Answer } \$40 = 00$$

A Note was given December 8th 1804 for 50
Dollars with Interest until paid there were endor-
sements as follows Jan^y 4th 1805 25 Dollars
March 4th 1805 10 Dollars April 8th received
in full payment

$$\begin{array}{r} \text{Dec } 1804 \text{ --- } 0 \text{ --- } 4 \\ \text{Jan } 1805 \text{ --- } 1 \text{ --- } 8 \\ \hline = 0 = 26 \end{array}$$

$$\begin{array}{r} 2/50 \\ 25 \\ \hline 5/6 \end{array} \text{ } 3/6 \text{ is the fraction of } 25 \text{ days}$$

$$\begin{array}{r} 5/125 \\ 120 = 8 \end{array}$$

$$\begin{array}{r} \text{March } 1804 = 2 - 4 \\ 1804 - 0 - 4 \\ \hline 2 = 0 \end{array}$$

$$\begin{array}{r} \text{H. A. Miller} \\ 50 - 00 - 0 \\ 00 - 20 - 8 \\ \hline 50 = 20 = 8 \\ 25 - 00 - 0 \\ \hline 2/25 = 20 \text{ } 8 \\ 12 - 50 - 4 \\ \hline 25/20 - 8 \text{ Int. for 2 months} \end{array}$$

$$\begin{array}{r} 1804 = 3 - 8 \\ 1804 - 2 \text{ } 4 \\ \hline 1 = 4 \end{array}$$

$$\begin{array}{r} 25 = 20 - 8 \\ 25 - 2 \end{array}$$

$$\begin{array}{r} 23 = 46 = 0 \\ 10 - 000 \end{array}$$

$$2/15 = 46 = 0$$

$$7/7 = 73 = 0$$

$$1 - 10 = 4$$

$$8 = 834$$

$$15 = 46$$

$$2 - 08 = 8$$

$$15 \text{ } 84 \text{ } 8$$

Remains due on the

Note

Continued

Suppose A note gives Jan. 1st 1823 for
 320 Dollars and Interest at 6 per cent and 50
 Dollars were endorsed the first of July following
 and 150 Dollars the first of January 1825
 what is due on said note the first of April
 1827

$$\begin{array}{r} 1806 = 3-1 \\ 1802 = 8-1 \\ \hline 3 = 9 = 0 \end{array}$$

$$\begin{array}{r} 1806 = 3-1 \\ 1802 = 8-1 \\ \hline 4 = 9 = 0 \end{array}$$

$$\begin{array}{r} \text{H} \\ 320 \\ 6 \\ \hline 4/1920 \\ 7680 \\ 480 \\ \hline 8160 \end{array} \quad \begin{array}{r} \text{H} \text{ etc} \\ 320 \\ 89 = 60 \\ \hline 401 = 60 \end{array}$$

$$\begin{array}{r} 1806 = 9-1 \\ 1804 = 0-1 \\ \hline 2 = 9 = 0 \end{array}$$

$$\begin{array}{r} \text{H} \\ 50 \\ 6 \\ \hline 2/300 \\ 900 \\ 2/150 \\ 75 \\ \hline 1125 \end{array}$$

$$\begin{array}{r} \text{H} \\ 50 \\ 11 = 25 \text{ Interest} \\ \hline 61 = 25 \end{array}$$

$$\begin{array}{r} \text{endorsement} \\ 61 = 25 \text{ Int} \\ 170 = 25 \\ \hline 231 = 50 \end{array}$$

$$\begin{array}{r} \text{H} \\ 150 \\ 6 \\ \hline 4/900 \\ 2 \\ \hline 1800 \\ 225 \\ \hline 2025 \end{array}$$

$$\begin{array}{r} \text{H} \text{ cents} \\ 150 = 00 \\ 20 = 25 \\ \hline 170 = 25 \end{array}$$

$$\begin{array}{r} 401 = 60 \text{ Amount of the} \\ 231 = 50 \text{ the sum of the} \\ \hline 170 = 10 \text{ endorse mts with} \\ \text{interest} \end{array}$$

Answer 170 = 10 cents

Continued

Suppose A note given Jan^{ry} 1st 1804 for
 500 Dollars Interest at 6 per cent 250 Dollars
 were ~~then~~ endorsed on it June 16th following
 and 200 Dollars the 14th of May 1805
 and the 14th April following 28
 how much remains due upon said note
 the 14th of May following

$$\begin{array}{r} \text{May } 1804 = - 4 = 14 \\ \text{Jan } 1803 = - 0 - 1 \\ \hline 1 = 4 = 13 \end{array}$$

$$\begin{array}{r} 1804 = 4 = 14 \\ 1803 \quad 5 = 16 \\ \hline = 10 = 28 \end{array}$$

$$\begin{array}{r} 1804 = 4 = 14 \\ 1804 \quad 0 = 14 \\ \hline 4 = 00 \end{array}$$

$$\begin{array}{r} 1804 = 4 = 14 \\ 1804 \quad 3 = 14 \\ 1 = \\ \hline 1804 = 4 = 14 \end{array}$$

$$\begin{array}{r} 2/28 \\ \hline 14 \end{array} \quad \begin{array}{r} 28 - \\ 00 - 14 \\ \hline 28 = 14 \end{array}$$

$$\begin{array}{r} 2/500 \\ \hline 3/3000 \\ \hline 1000 \\ \hline 3/250 \\ \hline 83 \\ \hline 16 \\ \hline 5 \\ \hline 4804 \end{array}$$

$$\begin{array}{r} 500 \\ 41 = 4 \\ \hline 541 = 4 \end{array}$$

$$\begin{array}{r} 2/250 \\ \hline 1250 \\ \hline 125 \\ \hline 1375 \end{array}$$

$$\begin{array}{r} 250 \\ 13 = 13 \\ \hline 263 = 75 \end{array}$$

$$\begin{array}{r} 200 \\ 2 \\ \hline 400 \end{array} \quad \begin{array}{r} 200 \\ 204 \\ \hline \end{array}$$

$$\begin{array}{r} 263 = 75 \\ 204 = 00 \\ 28 = 14 \\ \hline 495 = 89 \end{array}$$

endorsement
with Interest

Answer 45 1/2 15 cents

$$\begin{array}{r} 541 = 04 \\ 495 = 89 \\ \hline 45 = 15 \end{array}$$

Continued

Suppose A note given Jan^r 12th 1809 for
 \$ 500 Dollars on Demand with Interest from the
 date \$ 400 of was endorsed on it Jan^r 12 1808
 \$ 100 Jan^r 12th 1809 how much was the due

Jan ^r 1808 = 0 - 12	\$ 500	\$ 500	what was Int ^r
1806 = 0 - 12	12	60	
2 = 0 - 60	60/00	560	Amount of the prin

1808 - 0 - 12
 1807 - 0 - 12
 1 - 0 - 00

400
 24/00

400
 100
 24 Int^r
 524

590
 524
 66 Answer

\$ 36 remains due

For Value receiv^d I promised to pay John Hooker
 50 Dollars on Demand with Interest from the date
 Jan^r 1st 1808 receiv^d full payment the
 April 19 following required the Interest

April 1808 = 3 = 14 2/50
 1807 = 0 - 1 1 1/2
 3 = 18 2/25
 12 = 5
 2 = 5
 18050

Answer 80 cents

Brimfield March 10th 1804

For value received of James Brown I promised
 to pay him on order fifty Dollars & thirty days
 after date with Interest

Required the Interest 365 = 1 = 50 = 60

25
 1750

365/9000(24
 270
 1700
 1460
 365/2400(16
 2190

Ans 24 cents & 2 mil

Continued

86

Required the Interest of 500 Dollars for $4\frac{1}{2}$ Months at 6 per cent

$$\begin{array}{r} \$500 \\ \times 2\frac{1}{2} \\ \hline 1250 \\ 1125 \\ \hline 1250 \\ \times 11 = 25 \end{array}$$

Required the Interest of 3060 Dollars for 6 Months 10 Days at 6 per cent

$$\begin{array}{r} \$3060 \\ \times 3\frac{1}{6} \\ \hline 15180 \\ \times 43 = 3 \\ \hline 16023 = 3 \end{array}$$

Answer 160 = 23 = 3

160 23 = 3 As before

What is the Interest of 500 Dollars for $\frac{1}{2}$ month at 6 per cent

$$\begin{array}{r} \$500 \\ \times 2 \\ \hline 1000 \\ \times 25 \\ \hline 1250 \\ \hline 375 \end{array}$$

Answer \$3 = 75

What is the Interest of 1000 Dollars for $4\frac{3}{4}$ years at $3\frac{3}{4}$ per cent

$$\begin{array}{r} \$1000 \\ \times 3\frac{3}{4} \\ \hline 3000 \\ \times 5 \\ \hline 15000 \\ \times 250 \\ \hline 37500 \\ \times 4\frac{1}{4} \\ \hline 15000 \\ 1895 \\ \hline 178125 \end{array}$$

Answer \$178125

Discount

Examples

What must be discounted for the ready payment of 100 Dollars due 2 years at 6% per year

$$\begin{array}{r} 100 \\ 106 \\ \hline 1200 \end{array} \quad \begin{array}{r} 100 \\ 112 \\ \hline 112 \end{array} = 12 = 100$$

$$\begin{array}{r} 112 \overline{) 1200} \quad (10/7/14 \\ 112 \\ \hline 80,00 \\ 84 \\ \hline 160 \\ 112 \\ \hline 480 \\ 448 \\ \hline 32 \end{array}$$

$$\begin{array}{r} 100 \\ 10 \\ \hline 89 = 28 = 6 \end{array}$$

What is the present worth of 642 Dol due 18 months hence at 6% per year

$$\begin{array}{r} 642 \\ 7 \\ \hline 2 \overline{) 4494} \\ 2242 \\ \hline 6741 \end{array}$$

$$\begin{array}{r} 642 \\ 67 = 41 \\ \hline 909 = 41 = 642 \end{array}$$

$$\begin{array}{r} 13482 \\ 26264 \\ \hline 40446 \\ 7094 \overline{) 4527722} \quad (61 \\ 425616 \\ \hline 71262 \\ 70941 \\ \hline 321000 \quad (00 = 4 \\ 7094 \overline{) 321000} \\ 283764 \\ \hline 37236 \end{array}$$

$$\begin{array}{r} 642 - 00 \\ 61 - 00 - 4 \\ \hline 580 = 99 = 6 \end{array}$$

$$\begin{array}{r} 580 = 99 = 6 \end{array}$$

Barter

Examples

How much Wheat must I be given
at $\$1\frac{1}{2}$ per bushel in barter for 66
bushels of rye at 55 cents per bushel

$$\begin{array}{r}
 66 \\
 \times 85 \\
 \hline
 330 \\
 528 \\
 \hline
 5610 \quad (37) \\
 45 \\
 \hline
 111 \\
 105 \\
 \hline
 6 \\
 4 \\
 \hline
 524 \quad (1) \\
 13 \\
 \hline
 9 \quad 3 \\
 15 \quad 3
 \end{array}$$

(Ans 37 bushels, $\frac{3}{5}$)

How much of flour at 12 cents
per lb for $2\frac{1}{2}$ yds of broadcloth
at $\$2\frac{1}{2}$ per yd

$$\begin{array}{r}
 12 \text{ cents} \\
 2\frac{1}{2} \text{ yds} \\
 \hline
 30 \text{ cents} \\
 12 - \frac{1}{4} 00 \\
 \hline
 800 \\
 12/1000 \quad (83\frac{1}{3}) \text{ the answer} \\
 96 \\
 \hline
 40 \\
 36 \\
 \hline
 4\frac{4}{12} \quad \frac{1}{3}
 \end{array}$$

Required The quantity of flour at 8 cents
A lb Wheat must be given in barter for
12 lb of indigo at $\$2-50$ cents per lb

$$\begin{array}{r}
 2 = 50 \\
 12 \\
 \hline
 30 = 00
 \end{array}$$

$$\begin{array}{r}
 8/3000 \quad (375) \text{ the answer} \\
 24 \\
 \hline
 60 \\
 56 \\
 \hline
 40 \\
 40
 \end{array}$$

Loss and gain

Examples

If I buy sugar at 5¢ per yard and sell it again at 5 1/4¢ per yard what do I gain per cent or in buying out 1000 to the gain or loss per cent

$$\begin{array}{r} 5 \text{ --- } 4 \\ 5 \text{ --- } 0 \\ \hline 0 \text{ --- } 4 \end{array} \text{ gain } 10\%$$

$$\begin{array}{r} 5 \text{ --- } 4 \text{ --- } 100 \\ \hline 2000 \\ 4 \end{array} \begin{array}{r} 12 \\ 20 \\ 4 \end{array}$$

$$\begin{array}{r} 5 \overline{) 16000} \quad 3200 \quad 266 \overline{) 13} \\ \underline{15} \quad \underline{24} \quad \underline{20} \\ 10 \quad 80 \quad 66 \\ \underline{10} \quad \underline{22} \quad \underline{60} \\ 00 \quad 80 \quad 60 \\ \underline{22} \end{array}$$

Ans. 13 1/2 60 1/4

$$\begin{array}{r} 5 \text{ --- } 4 \\ 5 \text{ --- } 0 \\ \hline 0 \text{ --- } 4 \end{array}$$

$$\begin{array}{r} 5 \text{ --- } 4 \text{ --- } 100 \\ \hline 12 \\ 68 \end{array}$$

$$\begin{array}{r} 24000 \\ 4 \end{array} \begin{array}{r} 12 \\ 20 \end{array}$$

$$\begin{array}{r} 68 \overline{) 192000} \quad 2823 \quad 235 \overline{) 11} \\ \underline{136} \quad \underline{24} \quad \underline{20} \\ 560 \quad 42 \quad 35 \\ \underline{544} \quad \underline{36} \quad \underline{20} \\ 160 \quad 69 \quad 15 \\ \underline{136} \quad \underline{60} \\ 240 \quad 3 \\ \underline{204} \\ 36 \\ \underline{34} \\ 2 \end{array}$$

Ans. 11 = 15 = 3 1/2

Continued

If I buy it at cost of the barco for £9-6-8
and sell it again at 1/10 per lb. I gain
or lose and what per cent

$$\begin{array}{r} 10 \\ 12 \\ \hline 22 \end{array}$$

$$\begin{array}{r} 22 \\ 12 \\ \hline 34 \end{array}$$

$$\begin{array}{r} 10-5-4 \\ 9-6-8 \\ \hline 18=8 \end{array}$$

$$\begin{array}{r} 224 \\ 12 \overline{) 2464} \\ \underline{24} \\ 64 \\ \underline{60} \\ 4 \end{array}$$

$$\begin{array}{r} 10-5-4 = 18=8 = 180 \\ 12 \\ \hline 380 \\ 186 \\ \hline 2240 \end{array}$$

$$\begin{array}{r} 12 \\ 44 \\ \hline 18 \\ 224 \end{array}$$

$$\begin{array}{r} 224 \overline{) 537600} \\ \underline{448} \\ 896 \\ \underline{896} \\ 00 \end{array}$$

$$20 \overline{) 2200} (10 \text{ at } 20$$

Confined Life and Gain

I have bought 60 yds of cloth at 280
per yd and 38 yds of do at 140 per yd
and sold them one with another at 260
per yd did I gain or lose and
what per cent

$$\begin{array}{r} \text{yd} \quad \text{yd} \quad \text{yd} \quad \text{yd} \quad \text{yd} \\ 1 - 28 - 60 \quad 1 = 14 - 38 \\ \hline 240 / 1680 \\ \hline 84 \end{array}$$

$$\begin{array}{r} 240 / 552 \\ \hline 26 - 12 \end{array} \quad \begin{array}{r} 26 = 12 \\ 84 - 00 \\ \hline 110 = 12 \end{array}$$

$$\begin{array}{r} 60 \\ 38 \\ \hline 98 \text{ yds} \end{array}$$

$$\begin{array}{r} 1 - 26 - 98 \\ \hline 127 = 8 \\ 110 - 12 \\ \hline 16 = 16 \text{ Answer} \end{array}$$

$$\begin{array}{r} 110 - 12 \\ \hline 20 \\ 2212 \end{array} \quad \begin{array}{r} 16 - 16 = 100 \\ \hline 20 \\ 2000 \end{array}$$

$$\begin{array}{r} 2212 / 672000 \quad 20 \\ \hline 5636 \quad 20 \\ 8400 \quad 103 \\ 6636 \quad 100 \\ \hline 1764 \quad 3 \\ 12 \\ 3528 \\ 1764 \\ \hline 2212 / 21168 \quad 9 \\ \hline 19208 \\ 1260 \\ 4 \end{array}$$

$$\begin{array}{r} 2212 / 5040 \quad 2 \\ \hline 4424 \\ 616 \end{array}$$

Ans 15-4
309 1/2

Continued

92

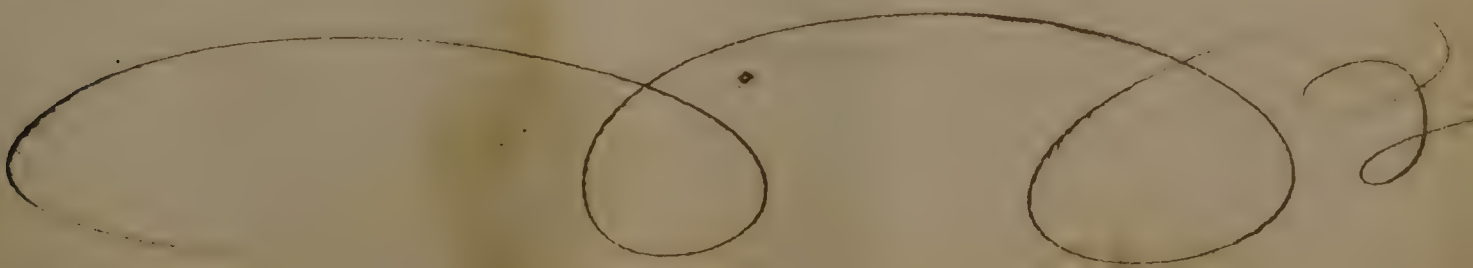
If $19\frac{1}{2}$ cwt of sugar be sold at $4\text{ £ } 5\text{ s}$ per cwt and I gain 15 per cent what did it cost per cwt

$$\begin{array}{r} \text{£} \quad \text{£ } s \quad \text{£} \\ 100 \quad - 4 - 5 = 100 \\ \underline{115} \quad \underline{20} \quad 20 \\ \quad 85 \quad 20 \\ \quad \underline{100} \\ 115 \overline{) 8500} (73 \text{ } 3 \\ \quad 805 \quad \underline{50} \\ \quad 450 \quad 13 \\ \quad \underline{345} \\ \quad 105 \\ \quad \underline{112} \\ \quad 40 \\ \quad 105 \\ 115 \overline{) 1260} (10 \\ \quad 115 \\ \quad \underline{110} \\ \quad 4 \\ 115 \overline{) 440} (3 \\ \quad 345 \\ \quad \underline{95} \quad 19 \\ 5 \overline{) 115} 23 \end{array}$$

Answer $\text{£ } 3 \text{ } 13 \text{ } 10 \text{ s } 3 \frac{19}{23}$

If both sold at $5\frac{1}{8}$ per cwt be $\text{£ } 13 - 6\frac{7}{8}$ profit per cwt. What gain or loss per cwt shall I have if I sell the same at 5 s per cwt

$$\begin{array}{r} \text{£ } s \quad \text{£} \quad \text{£} \quad \text{£} \\ 5 - 8 = 100 = 5 \quad 5 \\ \underline{12} \quad \underline{13} = 5 - 8 \quad \underline{12} \\ 68 \quad 113 - 5 - 8 \quad 50 \\ \quad 20 \\ \quad 226 \\ \quad \underline{12} \\ \quad 4540 \\ \quad 2265 \\ \quad \underline{27200} \quad 12 \quad 20 \quad \text{£} \\ 68 \overline{) 1632000} (24000 (2000 (100 \\ \quad 136 \quad \underline{24000} \\ \quad 272 \quad 20 \\ \quad \underline{272} \\ \quad 000 \end{array}$$



Square Root

Examples

Required the square root of 30138696025

$$\begin{array}{r}
 173605 \text{ Answer} \\
 1 \overline{) 30138696025} \\
 \underline{201} \\
 189 \\
 \underline{1238} \\
 1029 \\
 \underline{20969} \\
 20726 \\
 \underline{1736025} \\
 1736025
 \end{array}$$

Required the square root of 5755

$$\begin{array}{r}
 2398 \text{ The root Required} \\
 2 \overline{) 5755} \\
 \underline{4} \\
 43 \\
 \underline{129} \\
 469 \\
 \underline{422} \\
 4788 \\
 \underline{38304} \\
 4596 \text{ Remainder}
 \end{array}$$

Required the root of 96410342656

$$\begin{array}{r}
 3216 \text{ And the root Required} \\
 3 \overline{) 96410342656} \\
 \underline{9} \\
 62 \\
 \underline{184} \\
 641 \\
 \underline{124} \\
 641 \\
 \underline{641} \\
 6426 \\
 \underline{38556} \\
 38556
 \end{array}$$

Continued

What is the square root of 964, 5192360241

$$\begin{array}{r}
 3 \overline{) 964, 5192360241} \quad (31, 05671 \text{ Ans.} \\
 \underline{9} \\
 61 \\
 \underline{5205} \\
 62106 \\
 \underline{31025} \\
 621127 \\
 \underline{416736} \\
 6211341 \\
 \underline{372636} \\
 6211341 \\
 \underline{4410002} \\
 6211341 \\
 \underline{4347889} \\
 6211341 \\
 \underline{6211341} \\
 6211341 \\
 \underline{6211341}
 \end{array}$$

What is the square root of 0000316969

$$\begin{array}{r}
 0 \overline{) 0000316969} \quad (00563 \text{ Answer} \\
 \underline{00} \\
 00 \\
 \underline{0000} \\
 005 \\
 \underline{31} \\
 106 \\
 \underline{25} \\
 1123 \\
 \underline{569} \\
 1123 \\
 \underline{536} \\
 1123 \\
 \underline{3369} \\
 1123 \\
 \underline{3369}
 \end{array}$$

What is the root of 625

$$\begin{array}{r}
 2 \overline{) 625} \quad (25 \\
 \underline{4} \\
 45 \\
 \underline{225} \\
 225 \\
 \underline{225}
 \end{array}$$

25 is the root Required

25
Pulgar Fractions and mixed numbers
Example

What is the square root of $\frac{144}{15129}$

$$\begin{array}{r} 3 \\ 3 \overline{) 144} \\ \underline{15129} \end{array}$$

$$\begin{array}{r} 48 \\ 48 \\ \underline{5048} \end{array}$$

$$\begin{array}{r} 16 \\ 16 \\ \underline{1681} \end{array}$$

$4 \overline{) 16}$ 4 root of the numerator

$$\begin{array}{r} 4 \overline{) 1681} \\ \underline{16} \\ 81 \\ \underline{81} \end{array}$$

41 root of the denominator

Therefore $\frac{4}{41}$ is the root of the given fraction.

What is the square root of $\frac{1764}{5184}$

$$\begin{array}{r} 6 \\ 6 \overline{) 1764} = 294 = 49 \\ \underline{5184} = 864 \end{array}$$

$$\begin{array}{r} 7 \overline{) 49} \\ \underline{49} \end{array}$$

7 the root

$$\begin{array}{r} 12 \\ 12 \overline{) 144} \\ \underline{144} \end{array}$$

$\frac{7}{12}$ Answer



Continued

What is the square root of $42\frac{1}{4}$

$$\begin{array}{r} 42\frac{1}{4} \\ \underline{169} \\ 4 \end{array} \quad \begin{array}{r} 1/169(13 \\ \underline{1} \\ 69 \\ \underline{69} \end{array} \quad \begin{array}{r} 2/4(2 \\ \underline{4} \end{array}$$

$$\begin{array}{r} 2/13 \\ \underline{6\frac{1}{2}} \end{array} \text{ Answer}$$

Application and use of the Square Root

Problem 1st

Examples

What is the mean proportional between 24 and 96

$$\begin{array}{r} 96 \\ \underline{24} \\ 384 \\ \underline{192} \\ 2304 \end{array} \quad \begin{array}{r} 4/2304(48 \text{ Answer} \\ \underline{16} \\ 704 \\ \underline{704} \end{array}$$

Problem 2nd

Examples

If the area of a circle be 184,125 what is the side of a square equal in area there to

$$\begin{array}{r} 1/184,125(13,56 + \text{Answer} \\ \underline{1} \\ 23 \quad 84 \\ \underline{69} \\ 25 \quad 1512 \\ \underline{1305} \\ 2702 \quad 18750 \\ \underline{16235} \\ 2514 \end{array}$$

Continued

If the area of a triangle be 160 what is the side of a square equal in area.

1	160	(12, 64 + Answer
22	60	
246	44	
	1600	
	1476	
2524	12400	
	10096	
	2304	

Problem 3rd

Examples

A certain General has an army of 5625 men. In how many must he place in rank and file to form them in a square

7	5625	(75
	49	
145	725	
	725	

Problem 4th

Examples

Let 10952 Men be so formed so that the number in rank may be double the file

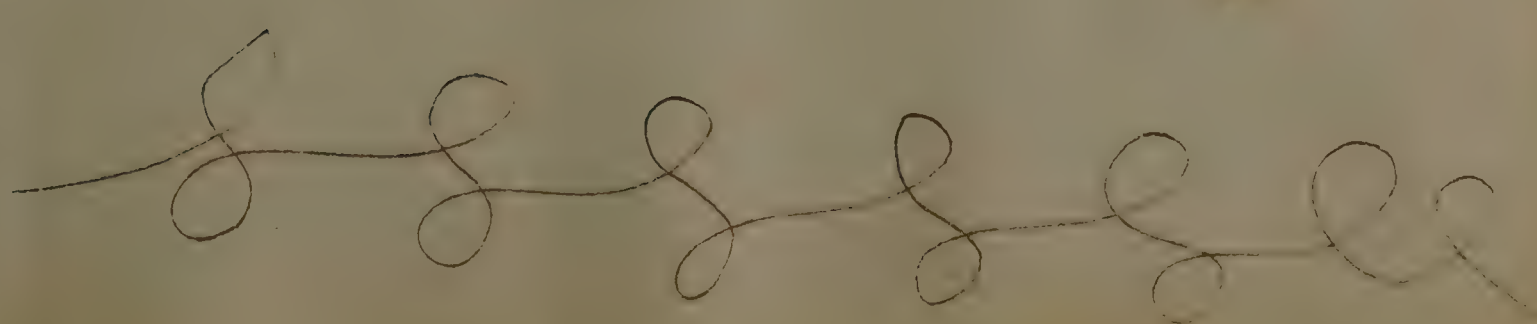
$$\begin{array}{r} 2 \overline{) 10952} \\ 5476 \end{array} \quad \begin{array}{r} 7 \overline{) 5476} \text{ (7 in file)} \\ 49 \\ \hline 576 \\ 576 \end{array} \quad \begin{array}{r} 7 \overline{) 148} \text{ in rank} \\ 21 \\ \hline 148 \end{array}$$

Problem 5th

Examples

If it be required to place 2016 men so as that they may be 56 in rank and 36 in file and to stand 4 feet distance in rank and as much in file how much ground do they stand on

$$\begin{array}{r} 1-4 = 55 \\ 4 \\ \hline 220 \\ 140 \\ \hline 8800 \\ 220 \\ \hline 30800 \text{ feet Answer} \end{array} \quad \begin{array}{r} 56-1 \\ 1 \\ \hline 55 \end{array} \quad \begin{array}{r} 1-4 = 35 \\ 4 \\ \hline 140 \end{array} \quad \begin{array}{r} 36-1 \\ 1 \\ \hline 35 \end{array}$$



Problem 6th

Examples

Suppose I would set out an orchard of 600 trees so that the length shall be to the breadth as 3 to 2 and the distance of each tree one from the other 7 yards how many trees must it be in length and how many in breadth and how many square yards of ground do they stand on

$$\begin{array}{r} \text{As } 3-2-600 \\ \underline{3/1200} \\ 400 \end{array}$$

$$\begin{array}{r} 2/400 \text{ (20 the next)} \\ \underline{40} \\ 400 \end{array}$$

$$\begin{array}{r} 1=7 \dots 20 \text{ --- } 1 \\ \underline{19} \\ 1 \\ \underline{19} \\ 133 \end{array}$$

$$\begin{array}{r} \text{As } 2-3-600 \\ \underline{2/1800} \\ 900 \end{array}$$

$$\begin{array}{r} 3/900 \text{ (30)} \\ \underline{60} \\ 900 \end{array}$$

$$\begin{array}{r} 1=7=30 \text{ --- } 1 \\ \underline{29} \\ 29 \\ \underline{203} \\ 133 \end{array}$$

$$\begin{array}{r} 609 \\ \underline{203} \\ 26999 \text{ Square yds} \end{array}$$

Ans

Problem 7th

Examples

Admit A boiler pipe $\frac{3}{4}$ inch diameter will fill A cistern in 3 hours I demand the diameter of another pipe which will fill the same cistern in one hour

Reduce $\frac{3}{4}$ to A decimal

$$\frac{4}{3} \overline{) 3.75}$$

$$.75 \times 75$$

$$\begin{array}{r} \text{Ans } 325 \\ 3 \overline{) 975} \\ \underline{3625} \\ 35875 \end{array} \quad \text{Ans } 1 \text{ inverse}$$

$$1/1.5 \times 75 (129 + \text{Ans})$$

$$\begin{array}{r} 22 \overline{) 249} \\ \underline{44} \\ 2495 \\ \underline{2241} \\ 254 \end{array}$$

Problem 8th

Examples

If a pipe whose diameter is 1.5 of an inch fill A cistern in 5 hours in what time will a pipe whose diameter is 3.5 inches fill the same

$$\begin{array}{r} 1.5 \times 1.5 \\ 1.5 \\ \underline{75} \\ 15 \\ \underline{225} \end{array}$$

$$\begin{array}{r} 3.5 \times 3.5 \\ 3.5 \\ \underline{175} \\ 105 \\ \underline{1225} \end{array}$$

$$\begin{array}{r} 12,25 \overline{) 11250} \\ \underline{11025} \\ 2250 \\ \underline{1225} \\ 1025 \end{array}$$

$$\begin{array}{r} 31 \\ \underline{60} \\ 5660 \\ \underline{60} \\ 3600 \end{array}$$

54 minutes 36 seconds Ans

Problem 29th

Examples

If A pipe 6 inches bore will be 4 hours in running off A certain quantity of water in what time will 3 pipes each 4 inches bore be in discharging double the quantity

$$\begin{array}{r} 6 \times 6 \\ \hline 36 \end{array}$$

$$\begin{array}{r} 3 \times 4 \times 4 \\ \hline 48 \end{array}$$

$$\begin{array}{r} 36 - 48 = 12 \\ 12 \div 4 = 3 \\ 3 \times 4 = 12 \\ 12 \div 3 = 4 \text{ hours answer} \end{array}$$

Two ships sail from the same port one goes due north 45 leagues and the other due west 76 leagues how far are they asunder

$$\begin{array}{r} 45 \times 45 \\ \hline 2025 \end{array}$$

$$\begin{array}{r} 76 \times 76 \\ \hline 5776 \end{array}$$

$$\begin{array}{r} 7801 \text{ (44, 32)} \\ \hline 164 \\ 1763 \\ 17662 \end{array}$$

Answer 88, 32 + leagues

Single Fellowship

Examples

A man died leaving an estate of $148\text{ £ } 2\frac{1}{6}$
but he owes $21\text{ £ } 9\frac{1}{6}$ $572\text{ £ } 19\frac{1}{3}$ $614\text{ £ } 13\frac{1}{9}$ and $264\text{ £ } 17\frac{1}{6}$ & demand how
his estate must be divided Among his creditors

$$\begin{array}{r} 21 = 9 = 6 \\ 72 = 19 = 3 \\ 114 = 13 = 9 \\ 264 = 17 = 6 \\ \hline 474 = 10 = 0 \\ 20 \\ \hline 9480 \\ 12 \\ \hline 113760 \end{array}$$

$$\begin{array}{r} 113760 = 148 - 2 - 6 = 21 = 9 = 6 \\ 20 \\ \hline 2962 \\ 12 \\ \hline 5930 \\ 2962 \\ \hline 35550 \\ 5154 \end{array}$$

$$\begin{array}{r} 20 \\ \hline 429 \\ 12 \\ \hline 564 \\ 429 \\ \hline 5154 \end{array}$$

$$\begin{array}{r} 113760 \overline{) 183224} \quad 700 \quad \begin{array}{l} 12 \quad 20 \\ 1610 \end{array} \overline{) 134} \quad 6 \text{ £} \\ 113760 \\ \hline 694647 \\ 682560 \\ \hline 120870 \\ 113760 \\ \hline 71100 \\ 4 \end{array}$$

$$\begin{array}{r} 113760 \overline{) 284400} \quad 2 \text{ Ch } \\ 227520 \\ \hline 56880 \end{array}$$

As share $6\text{ £ } 14\frac{1}{2}$

$$\begin{array}{r} 113760 = 148 - 2 - 6 = 21 = 9 = 6 \\ 20 \\ \hline 2962 \\ 12 \\ \hline 5930 \\ 2962 \\ \hline 35550 \\ 5154 \end{array}$$

1751

35550

3 5 5 5 0

177750

248850

35550

113790

6225160

56880

537/4

45504

82 / 20
22

72650

24 88 3

2283

2153

25 share 22 1/2

$$113260 = 95550 - \frac{20}{14} = 93 - 9$$

2293

92

4595

8293

27 25

5550

137625

1376 25

137625

42575

11376/9785

91008

6 5 4 3 3

68252

1775

11/5/2

6399

11374 25 596 (2

22 152

2844

Do share £35 $\frac{2}{9}$

Continued

113760

35550

264 = 19-6

20
5297
12

10600
5297
63570
35550

317850

317850

317850

190716

113760

2259913500
11376
112231
102384

98473

91008

74655

68256

63990

56880

17174

11376/284440(2
22752
5688

Did share

92

19865 (1655)

12
74
72
66
60
65
60
5

2 15 5 1/2

52

20/1655(82 £
160
55
40
152

Anno's share --- £ 6 - 14 - 2 1/2

Bo's share --- 22 - 16 ---

Co's share --- 35 - 16 - 9

Do's share --- 82 - 15 - 5 1/2

£ 148 = 2 = 5 proof

Double Fellowship

Examples

Two merchants trade in company A puts in
£100 for months B 136 for 3 months
but by misfortune they lose £50 he must
they share the loss

$$\begin{array}{r} \text{£} \\ 100 \\ 4 \\ \hline 400 \end{array}$$

$$\begin{array}{r} \text{£} \\ 136 \\ 3 \\ \hline 408 \\ 400 \\ \hline 408 - 50 = 400 \end{array}$$

$$\begin{array}{r} 408 \overline{) 20000} (24 \\ 1616 \\ \hline 3840 \\ 3232 \\ \hline 608 \\ 20 \\ \hline 408 \overline{) 12160} (15 \end{array}$$

$$\begin{array}{r} 408 \overline{) 12160} (15 \\ 4080 \\ 4040 \\ \hline 40 \\ 4 \\ \hline 408 \overline{) 1480} (0 \end{array}$$

$$\begin{array}{r} \text{£} \quad \text{£} \quad \text{£} \\ 408 = 50 = 408 \\ 408 \overline{) 20400} (25 \\ 1616 \\ \hline 4240 \\ 4040 \\ \hline 200 \\ 20 \\ \hline 408 \overline{) 4000} (4 \\ 3232 \\ \hline 768 \\ 12 \\ \hline 1536 \\ 768 \\ \hline 408 \overline{) 1920} (11 \\ 408 \\ \hline 1136 \\ 808 \\ \hline 328 \\ 4 \\ \hline 408 \overline{) 1312} (1 \\ 408 \\ \hline 504 \end{array}$$

Answer, A's share of the loss
is £24 15/08
B's £25 4/11/4

Equation of Payments

Example

Covers \$300 Dollars to be paid as follows \$50 in 2 months \$100 in 5 months \$150 in 8 months but it is agreed to make but one payment of the whole Demand when short time must be

\$50	\$50	100		
100	100	500		
150		1200		
300		1800		
	\$1000			
	500			
	\$1500			
	1200			

300	1800	months
1800	1800	Ans

Covers A certain sum of money which is to be paid one half present one fourth in 4 months and the remainder in 8 months what is the equated time for the whole

Suppose	\$40	20	20
		4	8
		40	160
one half	40	160	
1/4	20	80	240
	20	240	
	80		

Answer 3 Months

May 7th 1809

Single Position

Examples

A school master being asked how many he had said if I had as many more as I now have $\frac{3}{4}$ as many $\frac{1}{2}$ as many $\frac{1}{4}$ and $\frac{1}{8}$ as many I should then have 435 of what number did his school consist

Suppose 40

40
60
40
20
10

$$290 = 435 - 40$$

$$290 \overline{) 34890} \begin{array}{r} 120 \\ 580 \\ 580 \\ 0 \end{array}$$

120
120
90
60
30
15

435 Proof

A person lent his friend A sum of money unknown to receive Interest for the same at 6 per cent for annum simple Interest and at the end of 12 years received for principal and Interest £60 what was the sum lent

Suppose 100

$$\begin{array}{r} 100 \\ 600 \\ 12 \\ \hline 5200 \end{array}$$

$$172 - 100 = 72$$

$$172 \overline{) 5200} \begin{array}{r} 30 \\ 5160 \\ 40 \\ \hline 00 \end{array}$$

Continued

A B and C joined their stocks and gained
 £350 of which A took up A certain sum
 B took up 4 times so much as A C 8 times
 so much as B what share of the gain
 had each

Suppose $\frac{1}{2}$ that A took up

A's $\frac{1}{2}$ $\frac{640}{740} = \frac{350}{20} = 20$

$740/5000(9 \frac{1}{2})$

$74/680(9 \frac{1}{2})$

$74/168(2)$

$74/80(10 \frac{1}{2})$

B's $\frac{1}{2}$ $740 - 350 = 80$

$740/2800(3 \frac{1}{2})$

$74/1240(15 \frac{1}{2})$

$74/772(9 \frac{1}{2})$

$74/672(9 \frac{1}{2})$

C's $\frac{1}{2}$ $740 - 350 - 640$

$740/2100$

$740/2240(302 \frac{1}{2})$

$74/1040(14 \frac{1}{2})$

$74/48(10 \frac{1}{2})$

$74/192(2 \frac{1}{2})$

Answers

A's share £9 = $9 \frac{1}{2} \times \frac{6}{74}$

B's share --- $37 = 16 \frac{1}{2} \times \frac{6}{74}$

C's share 302 $14 \frac{1}{2} \times \frac{44}{74}$

~~Ans 349 $18 \frac{1}{2} \times \frac{56}{74}$~~

~~Wrong~~

Continued

A B C and D spent 35 shillings at a
 meeting and being a little tipsy they agreed
 that A should pay $\frac{1}{3}$ B $\frac{1}{2}$ C $\frac{1}{3}$ D $\frac{1}{4}$ what
 did each pay in the above proportions

Suppose £0
 $\frac{40}{40}$
 30
 20
 15
 $\frac{105}{105} = 35 - 40$
 $105 \overline{) 1400} (13$
 $\underline{105}$
 350
 $\underline{315}$
 35
 $\underline{35}$
 0
 Answer $13\frac{1}{4}$
 $105 \overline{) 420} (4$
 $\underline{420}$
 0

$105 = 35 = 30$ share
 $\frac{30}{105 \overline{) 1050} (10$ shilling B.D
 $\underline{1050}$
 0

$105 = 35 = 20$
 $105 \overline{) 2100} (6$
 $\underline{630}$
 720
 $105 \overline{) 840} (8$
 $\underline{840}$
 0
 Answer $6\frac{1}{8}$

$105 = 35 = 15$
 $\frac{15}{105 \overline{) 225} (2$
 $\underline{210}$
 15
 $\underline{15}$
 0
 1240

Answer A $13\frac{1}{4}$
 B $10\frac{1}{2}$
 C $6\frac{1}{8}$
 D $5\frac{1}{4}$

A certain sum of money is to be divided between
 5 men in such a manner as that A shall have
 $\frac{1}{4}$ B $\frac{1}{5}$ C $\frac{1}{10}$ D $\frac{1}{20}$ and the remainder which is
 40 £ what is the sum

Suppose £0
 $\frac{40}{40}$
 20
 16
 8
 4
 $\frac{32}{32}$ sum
 $\frac{40}{40}$
 $32 - 40 = 40$
 $\frac{40}{32 \overline{) 3200} (100$ Answer
 $\underline{3200}$
 00

Continued,

A person after spending $\frac{1}{2}$ and $\frac{1}{3}$ of his money had
£ $26\frac{2}{3}$ left what had he at first

Suppose 60
 $\frac{30}{20}$
 $\frac{50}{50}$

subtract 50 from $\frac{60}{50}$
 $\frac{10}{10}$

£ I £ I I I I
 $10 = 60 = 26 = 13 = 4$

$\frac{20}{200}$
 $\frac{12}{2400}$

$\frac{20}{533}$
 $\frac{12}{1070}$
 $\frac{533}{5400}$

$\frac{20}{340}$
 $\frac{13}{130}$

24/00 3840/00 160 £ Answer

A and B talking of their ages B said his age
was once and A half the age of A B said his was
twice and one tenth the age of both and that the
sum of their ages was 93 what was the age
of each

Suppose 40 years

$\frac{210}{310} - 40 = 93$

310/ 3720 12 Ans A 12 years

$\frac{31}{62}$
 $\frac{62}{62}$

$\frac{3}{12}$
 $\frac{6}{18}$ Ans Ans

A 12
 B 14
 C 63
 - 93 Proofs

$\frac{12}{18}$
 $\frac{10}{30}$
 $\frac{60}{3}$
 63 Ans Answer

Continued

$$\begin{array}{r} 60 \\ 30 \\ 15 \\ 20 \\ \hline 65-3-60 \\ 65-180 \end{array}$$

A vessel has 3 cocks A B and C. A can fill it in half an hour B in $\frac{1}{4}$ of an hour & C in $\frac{1}{3}$ of an hour in what time will they all fill it together

Minutes

Suppose 30.

$$\frac{1}{\frac{1}{2}} = 2$$

Min

$$\frac{2}{9} = \frac{30}{x} = \frac{1}{2}$$

$$9/60(6)$$

$$\frac{60}{60}$$

$$9/360(40)$$

Ans 6 Minutes 40

A person having about his A certain number of Dollars said that $\frac{1}{3}$ $\frac{1}{4}$ $\frac{1}{5}$ and $\frac{1}{6}$ of them would make 57 pray how many had he

Suppose 120

$$40$$

$$30$$

$$24$$

$$20$$

$$124 = 120 = 57$$

$$\frac{57}{124}$$

$$114/6840(60)$$

$$0$$

Answer

Continued

$$\begin{array}{r} 12 \\ 6 \\ 3 \\ 4 \\ \hline 13-3-12 \\ 3 \\ 13 \overline{) 36} (2 \\ \underline{26} \\ 100 \\ 13 \overline{) 600} (4 \\ \underline{52} \\ 80 \end{array}$$

A gentleman bought a chaise horse and harness for 100 £. The horse cost $\frac{1}{4}$ more than the harness and the chaise $\frac{1}{3}$ more than the horse what was the price of each

Suppose 24

$$\begin{array}{r} 30 \\ 40 \\ \hline 94 = 24 = 100 \end{array}$$

$$\begin{array}{r} 94 \overline{) 2400} (25 \text{ £ the harness cost} \\ \underline{188} \\ 520 \\ \underline{480} \\ 40 \\ \underline{38} \\ 20 \\ 94 \overline{) 1000} (10 \\ \underline{94} \\ 60 \\ \underline{58} \\ 20 \\ 94 \overline{) 520} (9 \\ \underline{658} \\ 62 \\ \underline{4} \\ 94 \overline{) 248} (2 \\ \underline{188} \\ 60 \\ \underline{58} \\ 20 \\ 94 \end{array}$$

$$\begin{array}{r} 94 = 30 = 100 \\ 94 \overline{) 3000} (31 \\ \underline{282} \\ 180 \\ \underline{94} \\ 86 \\ \underline{20} \\ 94 \overline{) 1720} (18 \\ \underline{94} \\ 780 \\ \underline{752} \\ 28 \\ 94 \overline{) 112} (1 \\ \underline{94} \\ 18 \\ 94 \overline{) 336} (3 \\ \underline{282} \\ 54 \\ 94 \overline{) 212} (2 \\ \underline{188} \\ 24 \\ 94 \end{array}$$

The horse 31 £ 18 13/2

$$440 = 11 = 0 3/4$$

$$\begin{array}{r} 94 = 40 = 100 \\ 94 \overline{) 4000} (42 \\ \underline{376} \\ 240 \\ \underline{188} \\ 52 \\ \underline{20} \\ 94 \overline{) 1040} (11 \\ \underline{94} \\ 100 \\ 94 \\ \underline{6} \\ 12 \\ 94 \overline{) 72} (0 \\ \underline{74} \\ 288 \\ 94 \overline{) 282} (3 \\ \underline{282} \\ 0 \\ 94 \end{array}$$

Continued Portion

A and B having found A purse of money
disputed who should have it A said the
 $\frac{1}{5}$ $\frac{1}{10}$ and $\frac{1}{20}$ of it amounted to 35 £ and
if B could tell him how much was in it
he should have the whole otherwise he should
have nothing how much did the purse contain

Suppose 60

$$\begin{array}{r} \frac{1}{5} \quad 12 \\ \frac{1}{10} \quad - 6 \\ \frac{1}{20} \quad 3 \\ \hline 21 \end{array}$$

$$21 = 60 = 35$$

$$\begin{array}{r} 300 \\ 150 \\ 21 \overline{) 2100} \quad (100 \text{ £ Answer} \\ \underline{2100} \\ 00 \end{array}$$

A gentleman divided his fortune Among his
sons to A he gave 9 £ as often as to B
to C 3 £ as often as to B 7 £ yet C
portion came to 1050 £ what was the
whole estate

Suppose 15 £

then A is 63 and B is 15 £

$$\begin{array}{r} A \text{ is } 63 \\ B \text{ is } 35 \\ C \text{ is } 15 \\ \hline 113 \end{array}$$

$$1050 \frac{4}{5}$$

$$\begin{array}{r} 40 \\ 5 \overline{) 200} \\ \underline{160} \end{array}$$

Continued

$$\begin{array}{r} 15 \\ 20 \\ \hline 300 \end{array} = 113 \frac{20}{1050} = 16$$

$$\begin{array}{r} 21016 \\ 113 \\ \hline 23048 \\ 21016 \\ \hline 21016 \\ 300 \overline{) 2374808} \quad 912 \\ \underline{2100} \\ 2748 \\ \underline{2700} \end{array}$$

$$1 \frac{3}{5}$$

Answer $7 \frac{9}{12} = 8$

$$\begin{array}{r} 480 \\ 300 \\ \hline 1808 \\ 1800 \\ \hline 808 \\ 20 \\ \hline 300 \overline{) 1600} \\ 12 \\ \hline 300 \overline{) 1920} \quad 6 \\ \underline{1800} \end{array}$$

$$\begin{array}{r} 120 \\ 4 \\ \hline 300 \overline{) 480} \quad 1 \\ \underline{300} \\ 180 \quad 30 \quad 8 \quad 3 \\ \hline 300 \quad 50 \quad 10 \quad 5 \end{array}$$

Seven eighths of a certain number exceeds $\frac{4}{5}$ by 6 what is that number

Ans. 40

$$\begin{array}{r} 40 \\ 8 \overline{) 280} \\ \underline{35} \end{array} \quad \begin{array}{r} 40 \\ 5 \overline{) 160} \\ \underline{32} \end{array} \quad \begin{array}{r} 35 \\ 32 \\ \hline 3 \end{array}$$

$$3 = 40 - 6$$

$$\begin{array}{r} 6 \\ 3 \overline{) 240} \\ \underline{80} \text{ Ans} \end{array}$$

$$\begin{array}{r} 40 \\ 8 \overline{) 320} \\ \underline{70} \end{array} \quad \begin{array}{r} 40 \\ 5 \overline{) 200} \\ \underline{64} \\ 2 \text{ added} \\ \underline{70} \end{array}$$

Continued

A having having a certain sum of money said
 $\frac{1}{2}$ $\frac{1}{3}$ and $\frac{1}{4}$ of it being added together
 made 13 $\frac{1}{4}$ what sum had he

Suppose 36

$$\begin{array}{r} \frac{1}{2} 18 \\ \frac{1}{3} 12 \\ \frac{1}{4} 9 \\ \hline 39 = 13 = 36 \end{array}$$

$$\begin{array}{r} 13 \\ 10.8 \\ \hline 33.8 \\ 39 \\ \hline 78 \\ 78 \end{array}$$

Done

Double Position

Examples

A lady bought damask for a gown at 4s per yard
 and lining for it at 3s per yd. the gown and lining
 contained 15 yds and the price of the whole
 was 3 £ 10s how many yds were there of each

Suppose 6 yds of damask then she must have
 9 of lining

$$\begin{array}{r} 48 \\ 27 \\ \hline 75 \\ 70 \\ \hline 5+ \end{array}$$

$$\begin{array}{r} 3 = 10 \\ 20 \\ \hline 70 \end{array}$$

Suppose 4 then 11

$$\begin{array}{r} 32 \\ 33 \\ \hline 65 \end{array}$$

$$\begin{array}{r} 70 \\ 65 \\ \hline 5- \end{array}$$

$$\begin{array}{r} 5 \\ 5 \\ \hline 10 \end{array}$$

Ans 5 yds of Damask
 10 yds of lining

$$\begin{array}{r} 4 \\ 20 \\ 30 \\ \hline 10 \end{array}$$

$$\begin{array}{r} 10 \\ 30 \\ \hline 40 \end{array}$$

Continued

2nd A and B have the same income A saves $\frac{1}{8}$ of his
 but B by spending 30 £ per annum more than
 A at the end of 8 years finds himself 40 £ in debt
 what is their income and what does each spend per
 annum

Suppose 80

$$\begin{array}{r} 1/8 \times 80 \\ \hline 10 \\ \hline 70 \end{array}$$

A spends 70 £

$$\begin{array}{r} 80 \\ \hline 10 \\ \hline 70 \\ \hline 30 \\ \hline 100 \end{array}$$

B - 100 £

$$\begin{array}{r} 80 \\ \hline 20 \\ \hline 8 \\ \hline 160 \\ \hline 40 \\ \hline 120 \end{array}$$

120 + error

Suppose 160 then 1/8 is 20

$$\begin{array}{r} 20 \\ \hline 140 \end{array}$$

A spends 140

$$\begin{array}{r} 30 \\ \hline 170 \end{array}$$

B spends

$$\begin{array}{r} 160 \\ \hline 10 \\ \hline 8 \\ \hline 80 \\ \hline 40 \\ \hline 40 \end{array}$$

Supposition

80 120 error

160 40 +

$$\begin{array}{r} 7200 \\ \hline 120 \\ \hline 19200 \\ \hline 3200 \\ \hline 16000 \end{array}$$

120

$$\begin{array}{r} 120 \\ \hline 40 \\ \hline 80 \end{array}$$

80 160 of 200 £ their incomes

$$\begin{array}{r} 160 \\ \hline 00 \end{array}$$

2

$$\begin{array}{r} 1/8 \times 200 \\ \hline 25 \end{array}$$

200

$$\begin{array}{r} 25 \\ \hline 175 \\ \hline 30 \\ \hline 205 \end{array}$$

A spends £ 175 and B £ 205

Sept 24th 1809

continued position, etc

What number is that, being increased
by its $\frac{1}{2}$ $\frac{1}{4}$ $\frac{1}{5}$ $\frac{1}{10}$ and $\frac{2}{3}$ of $\frac{3}{5}$ of $\frac{4}{8}$ and 7 will make

127 $\frac{1}{4}$

Suppose 160
80
40
32
~~28~~
7 $\frac{1}{4}$

327 $\frac{1}{4}$
127 $\frac{1}{4}$

200 + error

$\frac{2}{3}$ of $\frac{3}{5}$ of $\frac{4}{8}$ of 1

3
5

40
120

$\frac{5}{3}$

15
2

30

$\frac{5}{120}$ $\frac{6}{24}$ $\frac{1}{4}$

$\frac{1}{4}$ $\frac{7}{1}$

7
28

28
4/22

7 $\frac{1}{4}$

$\frac{1}{4}$ Divisor

Again Suppose 180
90
45
36
9
7 $\frac{1}{4}$

367 $\frac{1}{4}$
127 $\frac{1}{4}$

240 + second error

Supposition error

160	—	200 +	240
180	=	240	$\frac{200}{40}$ Divisor
<hr/> 16000		6400	
200		320	
<hr/> 36000		38400	
		36000	
		<hr/> 2400	60 Answer
		<hr/> 240	

60
30
15
12
3
7 $\frac{1}{4}$

127 $\frac{1}{4}$ Proof

CONTINUED

4th A and B laid out equal sums of money in trade A gained a sum equal to $\frac{1}{4}$ of his stock and B lost 225£ Then A's money was double that of B's what did each lay out

	$\frac{1}{4}$	£
Suppose	300	300
	75	225
	<u>375</u>	175
	150	75
Then	225	150

2 nd Suppose	900
	<u>225</u>
	1125

Supposition 300 225 error

900 ~~225~~

202500
67500

1500
6000

450/	270000	600	600
	<u>2700</u>		67500
	00		

900
<u>225</u>
675
675
<u>1350</u>
2125
<u>225</u>
error
225
<u>225</u>
450

£600 Answer

4th A Labourer was hired upon this condition that every day he wrought he should receive $\frac{3}{4}$ and for every day he was idle should forfeit $\frac{1}{4}$ £ At the expiration of the time he received $\frac{3}{15}$ how many days did he work & how many were he idle

Suppose 20 at 3-4 will be 40 hence

1-4	80
<u>20</u>	20
	40
	<u>80</u>
	80
	<u>80</u>
	00

12
<u>40</u>

20
<u>800</u>
3-15
<u>20</u>
175
<u>12</u>
1100

error

Continued Position

Again Suppose 40 --- 40 60
40
20 mile
20
400

$$\begin{array}{r} 1600 \\ 400 \\ \hline 1200 \\ 400 \\ \hline 1600 \end{array}$$

 20 ~~900~~ --- $\frac{900}{300} + \text{error}$
~~40~~ ~~300~~ +

$$\begin{array}{r} 36000 \\ 6000 \\ \hline 42000 \end{array}$$

$$\begin{array}{r} 900 \\ 300 \\ \hline 1200 \end{array}$$

$$\begin{array}{r} 1200 \overline{) 42000} \\ \underline{36} \\ 60 \\ \underline{60} \end{array}$$
 35
 I wonder 35 days he work'd 60
 All 35

6th

A gentleman has two horses of considerable value & a carriage worth 100 £ now if the first horse be sold & the carriage be put in it will be triple the value of the second but if the second be put in they will be 7 times the value of the first & the value of each horse

The first The second is
 worth 32 worth 44 £

$$\begin{array}{r} 100 \\ 3 \overline{) 132} \\ \underline{96} \\ 36 \end{array}$$

$$\begin{array}{r} 144 \\ 3 \overline{) 144} \\ \underline{132} \\ 12 \end{array}$$

$$\begin{array}{r} 148 \\ 1 \overline{) 148} \\ \underline{148} \end{array}$$

$$\begin{array}{r} 44 \\ 4 \overline{) 160} \\ \underline{160} \end{array}$$

Continued Position

120

Sup error
32 --- 80 ---

44 --- 160 ---

$$\begin{array}{r} 160 \\ 80 \\ \hline 80 \end{array}$$

$$\begin{array}{r} 320 \\ 320 \\ \hline 3520 \end{array}$$

$$\begin{array}{r} 1920 \\ 32 \\ \hline 5120 \\ 3520 \end{array}$$

8/0 16 0/0 20 the price of the 1st row

$$\begin{array}{r} 20 \\ 100 \\ 3 \overline{) 120} \\ \hline 40 \end{array}$$

£40 the price of the 2nd

7th There is a fish whose head is 10 feet long his tail is as long as his head and body the length of his body and his body is as long as his head and tail what is the whole length of the fish.

Suppose the body to be 20 feet long

2nd Sup. 30 --- 10
25
35
30
5 --- end

$$\begin{array}{r} 10 \\ 20 \\ 30 \\ 20 \\ \hline 10 \text{ --- end} \end{array}$$

Sup error
20 --- 10 ---
30 --- 5 ---

$$\begin{array}{r} 10 \\ 5 \\ \hline 5 \end{array}$$

$$\begin{array}{r} 300 \\ 100 \\ \hline 200 \end{array} = 100$$

5/200 40 the body 40 feet long

$$\begin{array}{r} 10 \\ 30 \\ 40 \\ \hline 40 \text{ feet body} \end{array}$$

Continued Section

What number is that which being increased by its $\frac{1}{2}$ its $\frac{1}{4}$ & more will be doubled

Suppose 8
 $\frac{1}{2}$
 $\frac{1}{4}$
 $\frac{1}{8}$
19
16
 3+

Suppose 16
 $\frac{1}{2}$
 $\frac{1}{4}$
 $\frac{1}{8}$
33
32
 1+ end

Sup. Error
 8 = 3+

16 = 1+

$\frac{3}{2}$ of 2 person

$\frac{48}{8}$

2/40 (20 Answer
40

(A man having driven his cattle to market received for them all £80 being paid at the rate of £4 per cow and £6 per calf. As £1 = 10 pence there were as many cows as cows & 4 times as many calves as cows & how many were there of each sort

Suppose 6 cows 6 cows 24 calves at £4 = 10
 $\frac{6}{36}$ $\frac{24}{96}$ $\frac{30}{36}$ 30 Shillings

$\frac{24}{36}$
 $\frac{36}{96}$
 $\frac{96}{80}$
16+

and Suppose 12

$\frac{12}{48}$
 $\frac{48}{72}$
 $\frac{72}{144}$
72

Sup. Error
 6 - - 16

$\frac{112}{16}$
96

$\frac{192}{140}$
112 + end

$\frac{12}{32}$
 $\frac{32}{16}$
192

$\frac{192}{192}$
480

96/480 (5 cows & 20 calves Answer
480

$\frac{5}{20}$

Position Continued

10th A B & C built a ship which cost them
£1000 of which A paid A certain sum B paid
£100 more than A & C £100 more than both
having finished her they put her for sea with a
cargo worth twice the value of the ship the
outfits and charges of the voyage amounted to
1/4 of the ship upon their return of which they
found their clear gain to be 2/3 of 3/5 of the value
of cargo & expenses please to inform me what
the ship cost them severally what share each
had in her & what upon the final adjustment
of their accounts they had severally gained

Suppose A paid £100

A	100
B	200
C	400
Total	700

2nd Suppose A paid £200

A	200
B	300
C	600
Total	1100
1000	
100 + Error	

Supposition Error

100	300 -
200	100 +
60000	
10000	
70000	
400	175
30	
24	
20	
20	

more than A 175
more than B 100
275

C 550
£ 550
1000

Division

300
100
400
175
275
450
600
550

Porter

Continued

$$\begin{array}{r} \text{£ ship £} \\ 1000 = 1 = 175 \\ 1000 \overline{) 1750} \end{array} \quad \begin{array}{r} \text{£} \\ 5/175 \quad 35 \quad 7 \\ \hline 1000 \quad 200 \quad 40 \end{array} \quad \text{Answer Answer } \frac{7}{40}$$

$$\begin{array}{r} \text{£} \\ 5/275 \quad 55 \quad 11 \\ \hline 1000 \quad 200 \quad 40 \end{array} \quad \text{Borrow } \frac{11}{40}$$

$$\begin{array}{r} \text{£} \\ 10/550 \quad 55 \quad 11 \\ \hline 1000 - 100 \quad 20 \end{array} \quad \text{Carry } \frac{11}{20}$$

They gained $\frac{2}{3}$ of $\frac{3}{5}$ $\frac{2}{3} \times \frac{3}{5} = \frac{2}{5}$ $\frac{2}{5} \times \frac{3}{5} = \frac{2}{5}$ $\frac{2}{5} \times \frac{3}{5} = \frac{2}{5}$ $\frac{2}{5} = \frac{3125}{5} = 1$

$\frac{1}{5} \times 1000 = 200$
 $\frac{1}{5} \times 200 = 40$
 $\frac{1}{5} \times 40 = 8$
 $\frac{1}{5} \times 8 = 1.6$
 $\frac{1}{5} \times 1.6 = 0.32$
 $\frac{1}{5} \times 0.32 = 0.064$
 $\frac{1}{5} \times 0.064 = 0.0128$
 $\frac{1}{5} \times 0.0128 = 0.00256$
 $\frac{1}{5} \times 0.00256 = 0.000512$
 $\frac{1}{5} \times 0.000512 = 0.0001024$
 $\frac{1}{5} \times 0.0001024 = 0.00002048$
 $\frac{1}{5} \times 0.00002048 = 0.000004096$
 $\frac{1}{5} \times 0.000004096 = 0.0000008192$
 $\frac{1}{5} \times 0.0000008192 = 0.00000016384$
 $\frac{1}{5} \times 0.00000016384 = 0.000000032768$
 $\frac{1}{5} \times 0.000000032768 = 0.0000000065536$
 $\frac{1}{5} \times 0.0000000065536 = 0.00000000131072$
 $\frac{1}{5} \times 0.00000000131072 = 0.000000000262144$
 $\frac{1}{5} \times 0.000000000262144 = 0.0000000000524288$
 $\frac{1}{5} \times 0.0000000000524288 = 0.00000000001048576$
 $\frac{1}{5} \times 0.00000000001048576 = 0.000000000002097152$
 $\frac{1}{5} \times 0.000000000002097152 = 0.0000000000004194304$
 $\frac{1}{5} \times 0.0000000000004194304 = 0.00000000000008388608$
 $\frac{1}{5} \times 0.00000000000008388608 = 0.000000000000016777216$
 $\frac{1}{5} \times 0.000000000000016777216 = 0.0000000000000033554432$
 $\frac{1}{5} \times 0.0000000000000033554432 = 0.00000000000000067108864$
 $\frac{1}{5} \times 0.00000000000000067108864 = 0.000000000000000134217728$
 $\frac{1}{5} \times 0.000000000000000134217728 = 0.0000000000000000268435456$
 $\frac{1}{5} \times 0.0000000000000000268435456 = 0.00000000000000000536870912$
 $\frac{1}{5} \times 0.00000000000000000536870912 = 0.000000000000000001073741824$
 $\frac{1}{5} \times 0.000000000000000001073741824 = 0.0000000000000000002147483648$
 $\frac{1}{5} \times 0.0000000000000000002147483648 = 0.00000000000000000004294967296$
 $\frac{1}{5} \times 0.00000000000000000004294967296 = 0.000000000000000000008589934592$
 $\frac{1}{5} \times 0.000000000000000000008589934592 = 0.0000000000000000000017179869184$
 $\frac{1}{5} \times 0.0000000000000000000017179869184 = 0.00000000000000000000034359738368$
 $\frac{1}{5} \times 0.00000000000000000000034359738368 = 0.000000000000000000000068719476736$
 $\frac{1}{5} \times 0.000000000000000000000068719476736 = 0.0000000000000000000000137438953472$
 $\frac{1}{5} \times 0.0000000000000000000000137438953472 = 0.00000000000000000000000274877906944$
 $\frac{1}{5} \times 0.00000000000000000000000274877906944 = 0.000000000000000000000000549755813888$
 $\frac{1}{5} \times 0.000000000000000000000000549755813888 = 0.0000000000000000000000001099511627776$
 $\frac{1}{5} \times 0.0000000000000000000000001099511627776 = 0.00000000000000000000000002199023255552$
 $\frac{1}{5} \times 0.00000000000000000000000002199023255552 = 0.000000000000000000000000004398046511104$
 $\frac{1}{5} \times 0.000000000000000000000000004398046511104 = 0.0000000000000000000000000008796093022208$
 $\frac{1}{5} \times 0.0000000000000000000000000008796093022208 = 0.00000000000000000000000000017592186044416$
 $\frac{1}{5} \times 0.00000000000000000000000000017592186044416 = 0.000000000000000000000000000035184372088832$
 $\frac{1}{5} \times 0.000000000000000000000000000035184372088832 = 0.0000000000000000000000000000070368744177664$
 $\frac{1}{5} \times 0.0000000000000000000000000000070368744177664 = 0.00000000000000000000000000000140737488355328$
 $\frac{1}{5} \times 0.00000000000000000000000000000140737488355328 = 0.000000000000000000000000000000281474976710656$
 $\frac{1}{5} \times 0.000000000000000000000000000000281474976710656 = 0.0000000000000000000000000000000562949953421312$
 $\frac{1}{5} \times 0.0000000000000000000000000000000562949953421312 = 0.00000000000000000000000000000001125899906842624$
 $\frac{1}{5} \times 0.00000000000000000000000000000001125899906842624 = 0.000000000000000000000000000000002251799813685248$
 $\frac{1}{5} \times 0.000000000000000000000000000000002251799813685248 = 0.0000000000000000000000000000000004503599627370496$
 $\frac{1}{5} \times 0.0000000000000000000000000000000004503599627370496 = 0.00000000000000000000000000000000009007199254740992$
 $\frac{1}{5} \times 0.00000000000000000000000000000000009007199254740992 = 0.000000000000000000000000000000000018014398509481984$
 $\frac{1}{5} \times 0.000000000000000000000000000000000018014398509481984 = 0.0000000000000000000000000000000000036028797018963968$
 $\frac{1}{5} \times 0.0000000000000000000000000000000000036028797018963968 = 0.00000000000000000000000000000000000072057594037927936$
 $\frac{1}{5} \times 0.00000000000000000000000000000000000072057594037927936 = 0.000000000000000000000000000000000000144115188075855872$
 $\frac{1}{5} \times 0.000000000000000000000000000000000000144115188075855872 = 0.0000000000000000000000000000000000000288230376151711744$
 $\frac{1}{5} \times 0.0000000000000000000000000000000000000288230376151711744 = 0.00000000000000000000000000000000000000576460752303423488$
 $\frac{1}{5} \times 0.00000000000000000000000000000000000000576460752303423488 = 0.000000000000000000000000000000000000001152921504606846976$
 $\frac{1}{5} \times 0.000000000000000000000000000000000000001152921504606846976 = 0.0000000000000000000000000000000000000002305843009213693952$
 $\frac{1}{5} \times 0.0000000000000000000000000000000000000002305843009213693952 = 0.004611686018427387904$
 $\frac{1}{5} \times 0.004611686018427387904 = 0.0009223372036854775808$
 $\frac{1}{5} \times 0.0009223372036854775808 = 0.00018446744073709551616$
 $\frac{1}{5} \times 0.00018446744073709551616 = 0.0036893488147419103232$
 $\frac{1}{5} \times 0.0036893488147419103232 = 0.00073786976294838206464$
 $\frac{1}{5} \times 0.00073786976294838206464 = 0.000147573952589676412928$
 $\frac{1}{5} \times 0.000147573952589676412928 = 0.00295147905179352825856$
 $\frac{1}{5} \times 0.00295147905179352825856 = 0.000590295810358705651712$
 $\frac{1}{5} \times 0.000590295810358705651712 = 0.001180591620717411303424$
 $\frac{1}{5} \times 0.001180591620717411303424 = 0.0002361183241434822606848$
 $\frac{1}{5} \times 0.0002361183241434822606848 = 0.0004722366482869645213696$
 $\frac{1}{5} \times 0.0004722366482869645213696 = 0.009444732965739290427392$
 $\frac{1}{5} \times 0.009444732965739290427392 = 0.00018889465931478580854784$
 $\frac{1}{5} \times 0.00018889465931478580854784 = 0.00037778931862957161709568$
 $\frac{1}{5} \times 0.00037778931862957161709568 = 0.00075557863725914323419136$
 $\frac{1}{5} \times 0.00075557863725914323419136 = 0.00151115727451828646838272$
 $\frac{1}{5} \times 0.00151115727451828646838272 = 0.00302231454903657293676544$
 $\frac{1}{5} \times 0.00302231454903657293676544 = 0.000604462909807314587353088$
 $\frac{1}{5} \times 0.000604462909807314587353088 = 0.001208925819614629174706176$
 $\frac{1}{5} \times 0.001208925819614629174706176 = 0.0002417851639229258349412352$
 $\frac{1}{5} \times 0.0002417851639229258349412352 = 0.0004835703278458516698824704$
 $\frac{1}{5} \times 0.0004835703278458516698824704 = 0.0009671406556917033397649408$
 $\frac{1}{5} \times 0.0009671406556917033397649408 = 0.0019342813113834066795298816$
 $\frac{1}{5} \times 0.0019342813113834066795298816 = 0.00038685626227668133590597632$
 $\frac{1}{5} \times 0.00038685626227668133590597632 = 0.00077371252455336267181195264$
 $\frac{1}{5} \times 0.00077371252455336267181195264 = 0.00154742504910672534362390528$
 $\frac{1}{5} \times 0.00154742504910672534362390528 = 0.000309485009821345068724781056$
 $\frac{1}{5} \times 0.000309485009821345068724781056 = 0.000618970019642690137449562112$
 $\frac{1}{5} \times 0.000618970019642690137449562112 = 0.001237940039285380274899124224$
 $\frac{1}{5} \times 0.001237940039285380274899124224 = 0.0002475880078570760549798248448$
 $\frac{1}{5} \times 0.0002475880078570760549798248448 = 0.0004951760157141521099596496896$
 $\frac{1}{5} \times 0.0004951760157141521099596496896 = 0.0009903520314283042199192993792$
 $\frac{1}{5} \times 0.0009903520314283042199192993792 = 0.0019807040628566084398385987584$
 $\frac{1}{5} \times 0.0019807040628566084398385987584 = 0.00039614081257132168796771975168$
 $\frac{1}{5} \times 0.00039614081257132168796771975168 = 0.00079228162514264337593543950336$
 $\frac{1}{5} \times 0.00079228162514264337593543950336 = 0.00158456325028528675187087900672$
 $\frac{1}{5} \times 0.00158456325028528675187087900672 = 0.000316912650057057350374175801344$
 $\frac{1}{5} \times 0.000316912650057057350374175801344 = 0.000633825300114114700748351602688$
 $\frac{1}{5} \times 0.000633825300114114700748351602688 = 0.001267650600228229401496703205376$
 $\frac{1}{5} \times 0.001267650600228229401496703205376 = 0.0002535301200456458802993406410752$
 $\frac{1}{5} \times 0.0002535301200456458802993406410752 = 0.0005070602400912917605986812821504$
 $\frac{1}{5} \times 0.0005070602400912917605986812821504 = 0.0010141204801825835211973625643008$
 $\frac{1}{5} \times 0.00101412048018258$

Position Continued

11th A B & C discussing of their money says
A I have 6 Dollars more than B says C I have
7 Dollars more than B well says A the sum of
our money is 100 Dollars how much has each one

What had B & C

A 6	100	2 nd Sub 20	26	100
B 12	37		33	79
C 19	69 - error		79	21 - error
37				

Sub error
6 = 63 -
20 = 21 -
2260 126
126
42/1134 (27)
84
294
294

63
21
42

27 A money
6
33 B's money
7
40 - C's

12th A man having been to market with hogs
pigs & geese received for them all 114 190 for
hogs he received 114 for every pig 75 cents
& for every goose 25 there were for every
pig 2 hogs & 3 geese what was the number
of each sort

Sub pose 12 hogs	24 pigs	36 geese
75	75	25
60	120	180
84	165	72
96	1800	900
190	24	
114	4	
76 -	96	

Sub pose 16 hogs 32 = 48
75 4 25
80 128 240
112 26
1200 1200 152 190
152 152
38 -

Portions continued

20
75
100
140
18/00

60
25
300
1200
18/00
40
160

end

Sub = 12 = 76 -

16 = 38 -

456
76
1216
456
760

76
38
38

20
2
40
3
120

38/760 (20 Answer 20 pigs

120 geese

20 x 3
3
60 geese

A man had an hundred pounds to be laid out in stock he will give 5 £ for oxen 1 £ for sheep & 1 £ for turkeys & wants 100 in the whole how many of each sort can he purchase with his money

Can he have 17 oxen Then he may have 80 turkeys
5
85
4
3
92
100
92
8 = end

Can he have 16 oxen 80 tur 4 sheep
5
80
4
4
88
100
88
12 = end

Sub end

17 = 8 -
16 = 12 -
128
34
162

12
8
4
120

304
128
4176 (19 Answer 19 oxen
36
36

Continued Division

16th Two men A & B having found a purse of money disputed who should have it A said he $\frac{1}{2}$ the $\frac{1}{3}$ and $\frac{1}{4}$ of the money made £130 and if B could have how much was in it he should have the whole otherwise he should have nothing I demand how much there was in it

Suppose $\frac{60}{30} \quad \frac{130}{65}$
 $\frac{20}{15}$
 $\frac{15}{65}$

Sub $\frac{36}{18} \quad \frac{130}{39}$
 $\frac{12}{9}$
 $\frac{9}{91}$

60
 36
 65-
 91-

91
 65
 26

390
 195
 2340

60
 540
 5460
 2340

26/3120(120
 26
 52
 52
 0

Answer £120

17th There are 2 numbers, the greatest is 3 times $\frac{4}{5}$ of the less, & the less is $\frac{1}{25}$, $\frac{1}{15}$, & $\frac{1}{5}$ of the greater & 1 besides
 What are those numbers? Ans 75 & 24

Compound Multiplication

Examples

What will 6 yards of cloth cost at $\$1-10-5$

per yard $\$1-10-5$
 $1 = 10 = 5$
 6

$\$9-2- = 6$ Answer

By federal money

$\$1-10-5 = 17$
 6
 $\$30-42$ Answer

Case 2nd

Examples

What will 42 yds of cloth
at $15/8$ per yd

$\$1-10-8$
 $0 = 15-8$
 6

$4 = 14 = 6$
 7

$\$93 = 7 = 6$ Answer

By federal money

cts
 $\$2-62-5$
 42
 $5-250$
 $105-00$
 $110-250$

Answer $\$110 = 25$ cts

Case 3rd Examples

What will 563 yds of cloth
cost at $\$2-1-6-7$ per yd

$\$2-1-6-7 \times 3$
 $1-6-7$

$13 = 5 = 10 \times 6$
 10

$132 = 18 = 4$
 5

$652 = 11 = 8$

$79 = 15 = 0$

$3 = 19 = 9$

$748 = 6 = 5$

Answer $\$748 = 6-5$

What will 51 yds of tea
at $3/6$ be

$\$1-10-8$
 $0-3-6$
 10

$1-18 = 0$
 5

$\$75 = 0$

$3-6$

$\$8 = 18 = 0$ Answer

Compound Division

Examples

If 5 yds of cloth cost £ 13 = 13/6 what is that per yd

$$\begin{array}{r} \text{£ } 13 = 13/6 \\ 5 \overline{) 13/6} \\ \underline{0 \quad 14} \quad 8 \quad 1 \end{array}$$

price per yard

If 35 yds of cloth cost £ 42 = 68/6 what is that per yd

$$\begin{array}{r} \text{£ } 42 = 68/6 \\ 35 \overline{) 42/68/6} \\ \underline{42} \quad 6 \quad 0 \quad 8 \quad 6 \\ \underline{60} \quad 8 \quad 6 \\ \underline{80} \quad 6 \end{array}$$

Answer

Case 2nd

Examples

If 1 cent of sugar cost £ 3 = 7 = 6 what is that per lb

$$\begin{array}{r} \text{£ } 3 = 7 = 6 \\ 8 \overline{) 3/7/6} \\ \underline{24} \quad 7 \quad 6 \\ \underline{24} \quad 7 \quad 6 \\ \underline{24} \quad 7 \quad 6 \\ \underline{24} \quad 7 \quad 6 \end{array}$$

Answer 7

Brimfield Feb^{ry} 1810

Continued

Divide £297 = 2/3 among 4 Men & Boys & give each man 3 times as much as one boy what will each man share and each boy

The men have thruple shares therefore multiply the number of men 4 by 3 and the number of boys 6 for a divisor

$$\begin{array}{r} 4 \\ 3 \\ \hline 12 \\ 6 \\ \hline 18 \text{ Divisor} \end{array}$$

$$\begin{array}{r} \text{£ } 297 \\ 18 \overline{) 297} \\ \underline{18} \\ 117 \\ \underline{108} \\ 90 \\ \underline{90} \\ 0 \end{array}$$

£ 16 = 10 = 1 = 2 = 1 boy share
3

£ 49 = 10 = 4 = 2 = 1 man share
4

198 = 1 = 6 = 0 Men
6

18 = 10 = 1 = 2 boy
6

99 = 0 = 9 = 0 boys
6

Part 297 = 2 = 3 = 0

Divide 39 = 12-5 among 4 men & women and 9 boys give each man double to a woman each woman double to a boy

$$\begin{array}{r} 4 \quad 6 \\ 4 \quad 12 \\ \hline 16 \quad 72 \\ 12 \\ \hline 9 \\ 37 \text{ Divisor} \end{array}$$

$$\begin{array}{r} \text{£ } 39 \\ 37 \overline{) 39} \\ \underline{37} \\ 20 \\ \underline{20} \\ 0 \end{array}$$

£ 12 = 1 = 1 = 5 = 1 boy share
2

2 = 2 = 10 = 1 woman share
2

4 = 5 = 8 = 1 man share
2

Feb 12 27 1809

Continued

Divide 5 guineas Among 8 men so that A shall have 8 more than B and B 8 more than C &c

$$\begin{array}{r} 5 \\ 28 \\ \hline 4 \overline{) 140} \\ 35 \end{array}$$

$$\begin{array}{r} 35 - 0 \\ 8 \\ \hline 2 \overline{) 34} = 4 \\ 19 - 2 \text{ C's share} \\ 8 \\ \hline 17 = 10 \text{ D's share} \\ 8 \\ \hline 18 = 6 \text{ E's share} \\ 8 \\ \hline 19 = 2 \text{ F's share} \\ 8 \\ \hline 19 = 10 \text{ G's share} \end{array}$$

to be 8's share on 6 to be

$$\begin{array}{r} 17 = 2 \text{ E's} \\ 8 \\ \hline 16 = 6 \text{ F's share} \\ 8 \\ \hline 15 = 10 \text{ G's share} \\ 8 \\ \hline 15 = 2 \text{ H's share} \end{array}$$

A	19 = 10
B	19 = 2
C	18 = 6
D	17 = 10
E	17 = 2
F	16 = 6
G	15 = 10
H	15 = 2
		<u>140 = 0</u>

$$\begin{array}{r} 28 \overline{) 140} (5 \text{ guineas} \\ 040 \end{array}$$

Dividing by 4 gets out the two middle ones shares which is D's and E's D has 8 more than E therefore subtract 8 from 35 D gets

out E's share and subtract 8 from 35 D gets out

28

~~On Thursday~~
~~4 1/2~~
 Divide $6 \overline{) 97} = 55 = 7 = 35 = 4 = 2 = 1 =$ by 6
 $16 \dots 20 \dots 7 = 12 = 8 = 11 = 1 = 1$
 6

$97 = 55 = 7 = 35 = 4 = 2 = 1$

When dividing this over we find that as $4 \frac{1}{2}$ miles is added to the 9 Furlongs that is less proving it must be subtracted from the furlongs and added to the miles and the $5 \frac{1}{2}$ feet that is reduced to inches must be subtracted and added to the feet

in this way $\frac{11}{6}$ 2 to carry from the Barley corn
 $\frac{6}{6} \frac{8}{8}$ 2
 $\frac{6}{6} \frac{6}{6}$ 2
 2 remain $5 \frac{1}{2}$ feet
 $\frac{2}{2}$
 $\frac{11}{6}$

then we say to the
 new figure 6×8
 $\frac{8}{6}$
 $\frac{48}{5 \frac{1}{2}}$ which must be added because taken from it

$164 \overline{) 53 \frac{1}{2}} (3$
 $\frac{48}{49 \frac{1}{2}}$
 $\frac{4}{4}$ Remainder 4 and 3 to carry to to next figure 12

Cube Root

Examples

Rule Take the nearest Root of the first period of the resolvend be it more or less than just and add to the right hand of it as many cyphers as there are remaining periods in the resolvend and call it the assumed root the multiply the given resolvend by 4 from the product subtract the cube of the assumed root Divide the remainder by 12 times the assumed root an extract the square root of the quotient back & the square Root & half the assumed root will give the answer

What is the cube root of 34965783

$$\begin{array}{r}
 34965783 \quad (300 \\
 \underline{4} \\
 139863132 \\
 \underline{27000000} \\
 3600/112863132 \quad (31350 \\
 \underline{10800} \\
 4863 \\
 \underline{3600} \\
 12631 \\
 \underline{10800} \\
 18313 \\
 \underline{18000} \\
 3132
 \end{array}$$

$$\begin{array}{r}
 300 \\
 \underline{12} \\
 3600 \text{ Divisor}
 \end{array}$$

$$\begin{array}{r}
 300 \\
 \underline{300} \\
 90000 \\
 \underline{300} \\
 27000000 \text{ the cube} \\
 \text{of the assumed root}
 \end{array}$$

$$\begin{array}{r}
 1/31350 \quad (177 \quad 2/300 \\
 \underline{1} \\
 213 \\
 \underline{189} \\
 2450 \\
 \underline{2421} \\
 21
 \end{array}$$

$$\begin{array}{r}
 177 \text{ the square root} \\
 150 \text{ half the assumed} \\
 \hline
 327 \text{ the root required}
 \end{array}$$

Continued

What is the cube root of 84,604,519

$$\begin{array}{r} 84,604,519 \quad (400 \\ \underline{4} \\ 338 \quad 418076 \\ \underline{64 \quad 000000} \\ 4800 \end{array}$$

$$\begin{array}{r} 400 \\ \underline{400} \\ 160000 \\ \underline{400} \\ 64000000 \end{array}$$

$$\begin{array}{r} 400 \\ \underline{12} \\ 4800 \text{ Divisor} \end{array}$$

$$\begin{array}{r} 274 \quad 418076 \quad (57170 \\ \underline{240000} \\ 34418 \\ \underline{33600} \\ 8180 \\ \underline{4800} \\ 33807 \\ \underline{33600} \\ 2076 \end{array}$$

$$\begin{array}{r} 2 \quad 57170 \quad (239 \\ \underline{4} \\ 48 \quad 171 \\ \underline{129} \\ 469 \quad 4270 \\ \underline{4221} \\ 49 \end{array}$$

239 The square
200 half the square

Answer 4039

Required the cube root of 373248

$$\begin{array}{r} 373248 \quad (70 \\ \underline{4} \\ 1492992 \\ \underline{343000} \\ 840 \end{array}$$

$$\begin{array}{r} 70 \\ \underline{70} \\ 4900 \\ \underline{70} \\ 840 \text{ Divisor} \end{array}$$

$$\begin{array}{r} 343000 \\ \underline{343000} \\ 0 \end{array}$$

$$\begin{array}{r} 840 \quad 1149992 \quad (1369 \\ \underline{8400} \\ 3099 \\ \underline{2520} \\ 5799 \\ \underline{5040} \\ 7592 \\ \underline{7560} \\ 32 \end{array}$$

$$\begin{array}{r} 3 \quad 114369 \quad (37 \\ \underline{9} \\ 67 \quad 469 \\ \underline{469} \\ 0 \end{array}$$

37 The square root
35 half the square root
72 the cube root required

Cube Root continued

What is the cube root of 843604519

$$\begin{array}{r}
 843604519 \quad 24.00 \\
 \underline{4} \\
 33 \ 8 \ 4180761 \\
 \underline{64} \quad 000000 \\
 4800 \overline{) 2744180761} \quad 57190 \\
 \underline{240000} \\
 34418 \\
 \underline{33600} \\
 8180 \\
 \underline{4800} \\
 33807 \\
 \underline{33600} \\
 2076
 \end{array}$$

$\frac{2400}{200}$ *Left of the square root*

$\frac{200}{239}$ *the square root*
 $\frac{4939}{4939}$ *the cube root*

[Signature]

$$\frac{7}{40} \quad \frac{11}{40} \quad \frac{11}{20}$$

$$7 \times 40 \times 20 = 560$$

$$11 \times 40 \times 20 = 880$$

$$11 \times 40 \times 40 =$$

280

440

20

